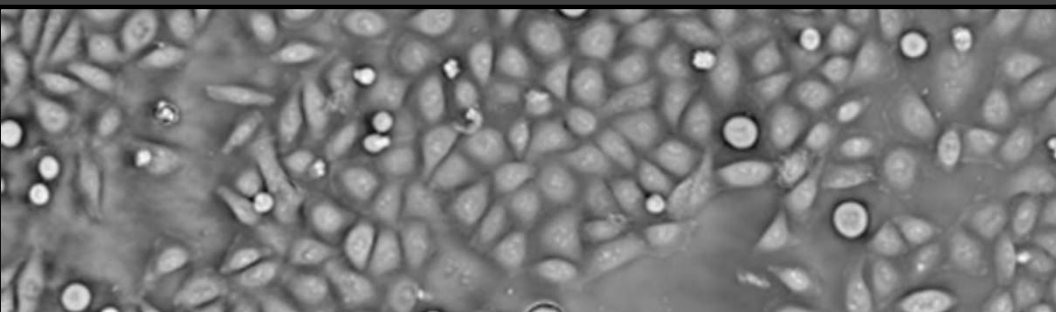


Laura Waller

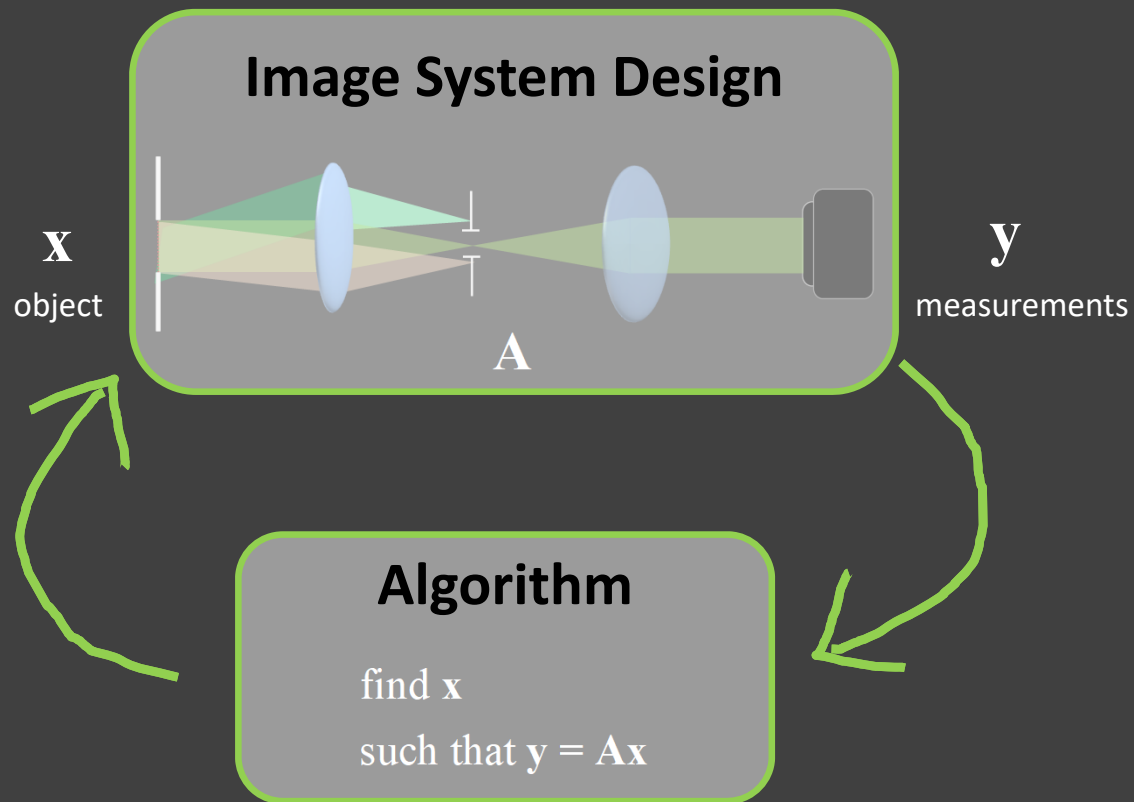
Electrical Engineering and Computer Sciences

UC Berkeley



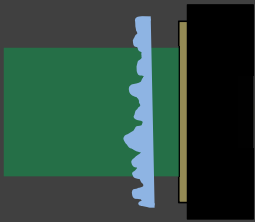
Computational Imaging

joint design of hardware and software

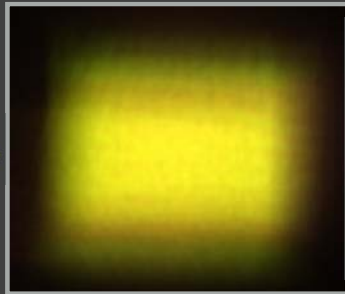


Computational imaging pipeline

Hardware design



Take picture



Crunch Data



Final result



The hard part is *integration*

Hardware Toolbox

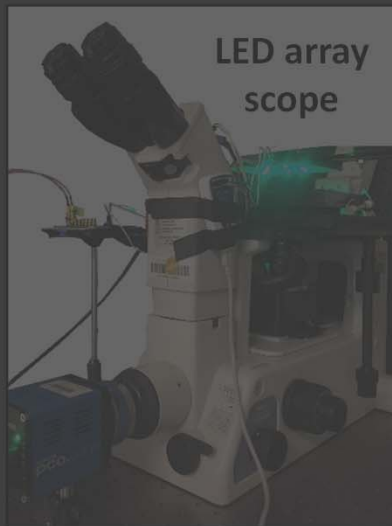


Computational Toolbox



Pushing the limits of imaging can be done with existing physics and commodity hardware.

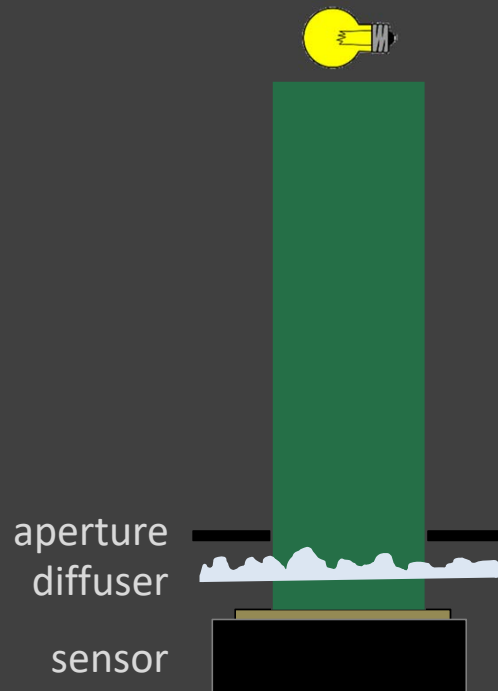
This talk:



- » *scalable* hardware
- » *efficient* data capture
- » *advanced computation*



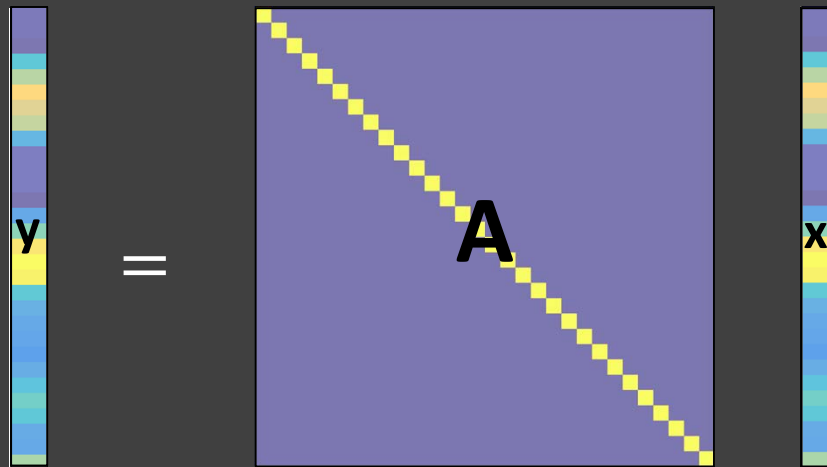
DiffuserCam: tape a diffuser onto a sensor



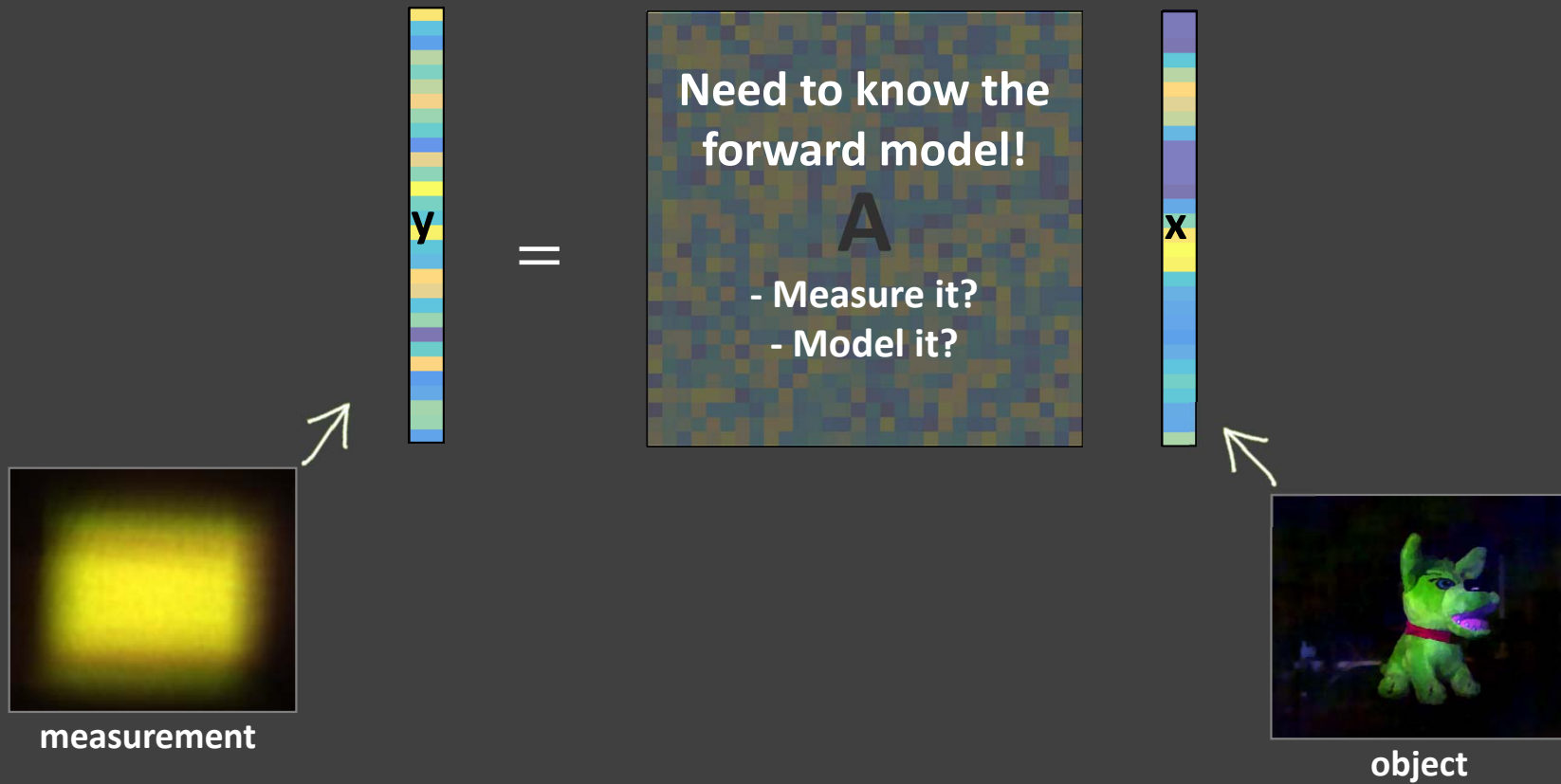
Grace Kuo
Nick Antipa



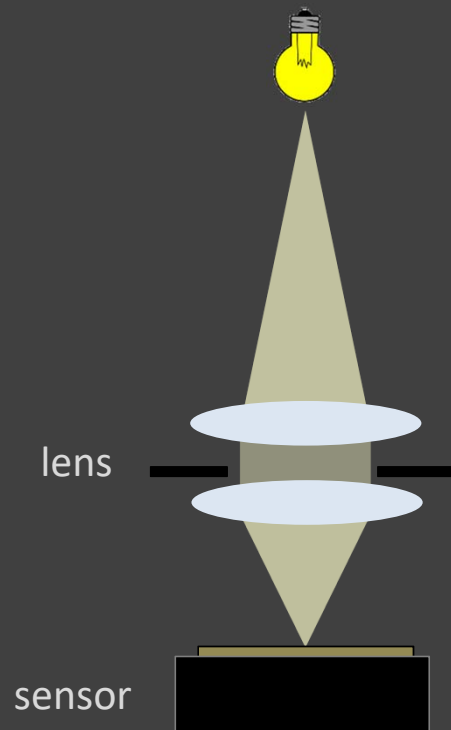
Traditional cameras take direct measurements



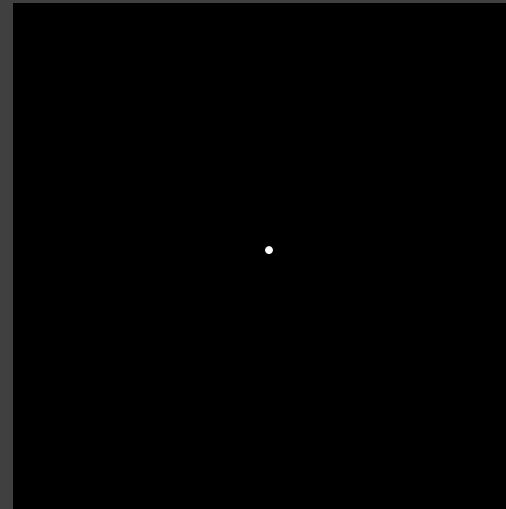
Computational cameras can multiplex



Lenses map points to points



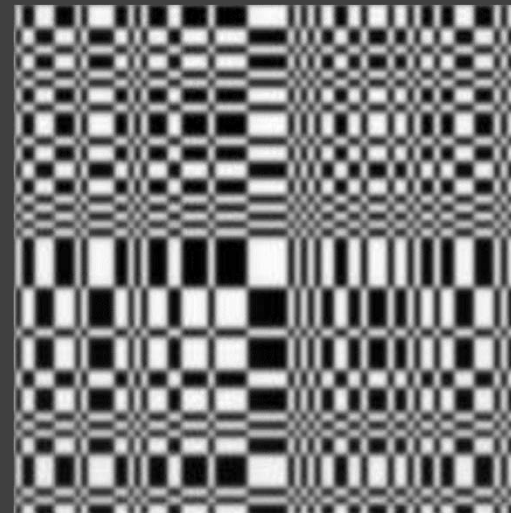
Point Spread Function (PSF)



Mask-based cameras multiplex

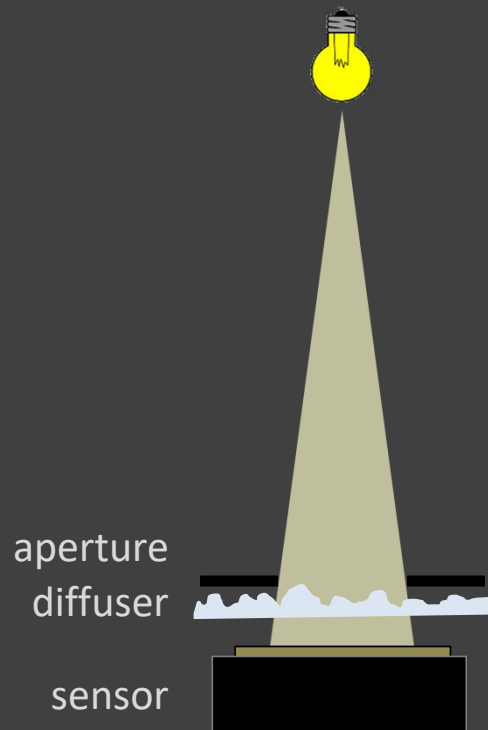


Point Spread Function (PSF)

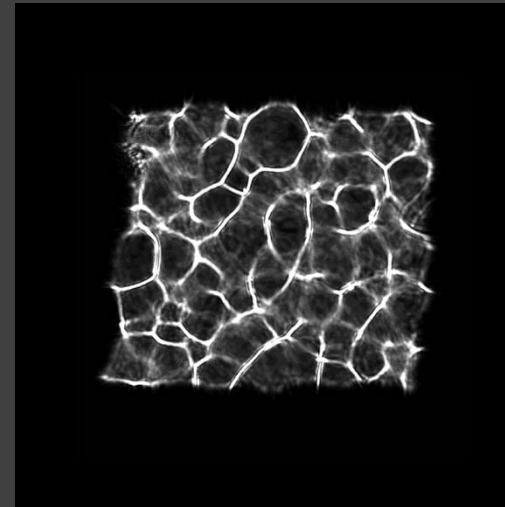


M. S. Asif, et al. *ICCVW* (2015)
J. Tanida, et al. *Applied optics* (2001)
K. Tajima, et al. *ICCP* (2017)
D. G. Stork, et al. *Int. J. Adv. Systems and measurements* (2014)

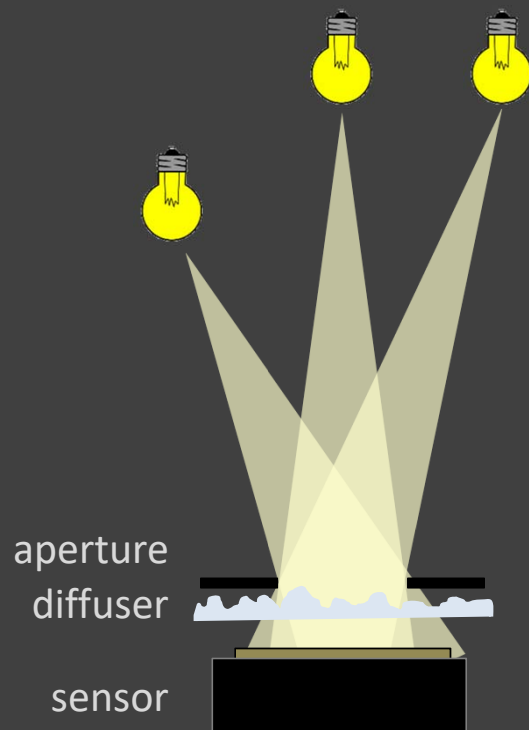
Diffuser indirectly encodes information



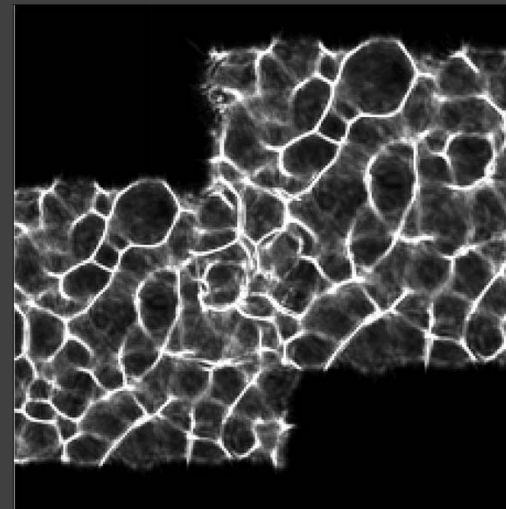
Point Spread Function (PSF)



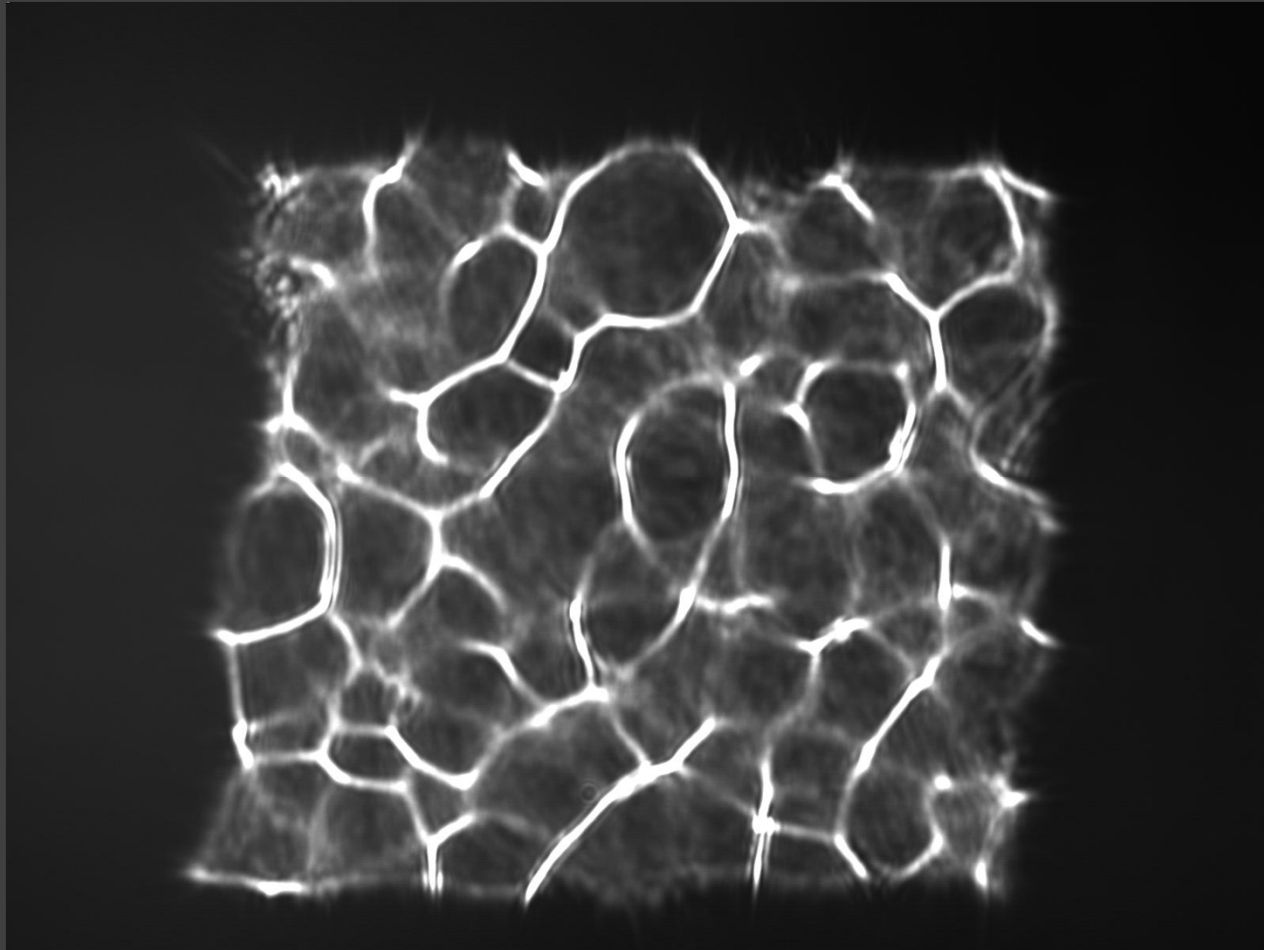
Diffuser indirectly encodes information



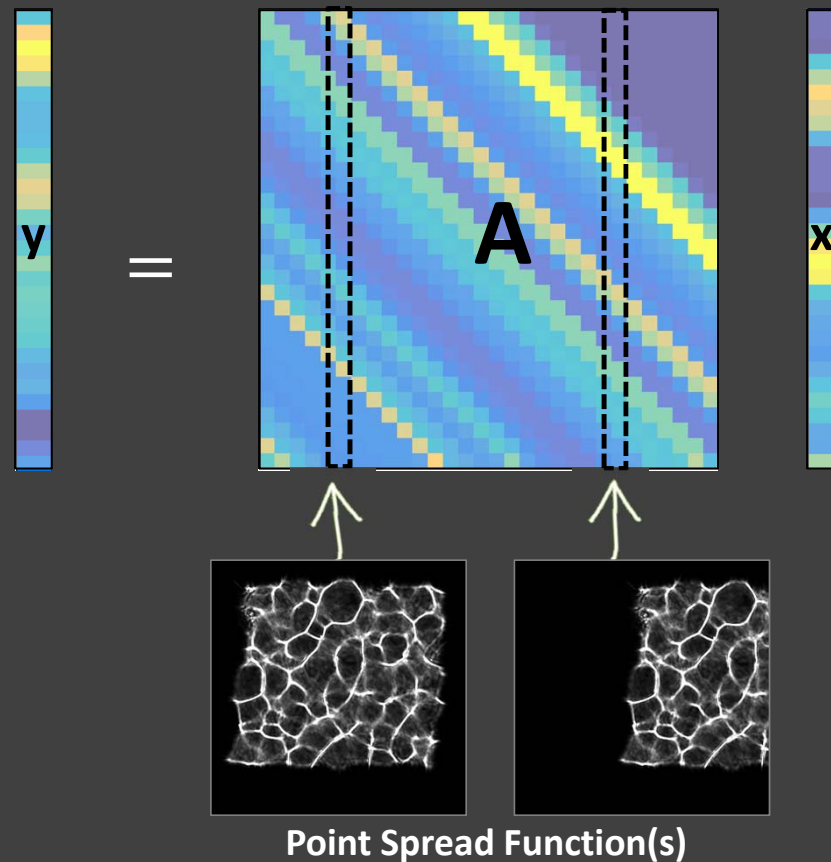
Point Spread Function (PSF)



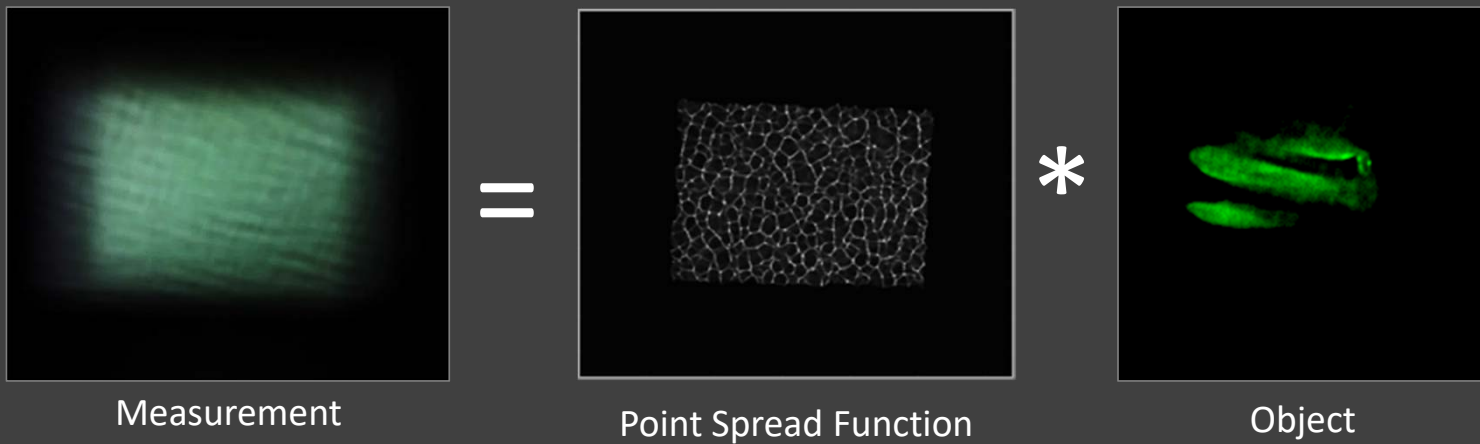
Point spread function shifts with the object



DiffuserCam forward model is a convolution



DiffuserCam forward model is a convolution





raw sensor data



recovered scene

*solver is ADMM with TV reg in Halide



raw sensor data



recovered scene

*solver is ADMM with TV reg in Halide



raw sensor data

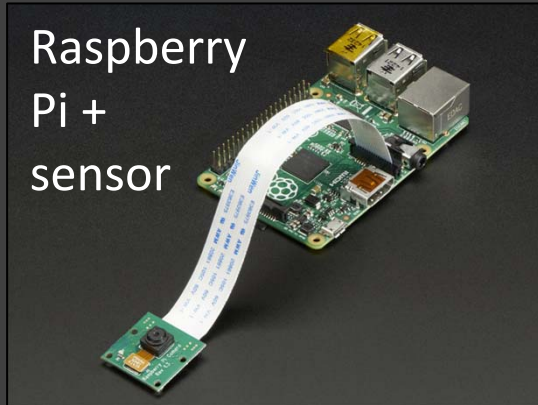


recovered scene

*solver is ADMM with TV reg in Halide

El cheapo version – ScotchTapeCam!

Raspberry
Pi +
sensor

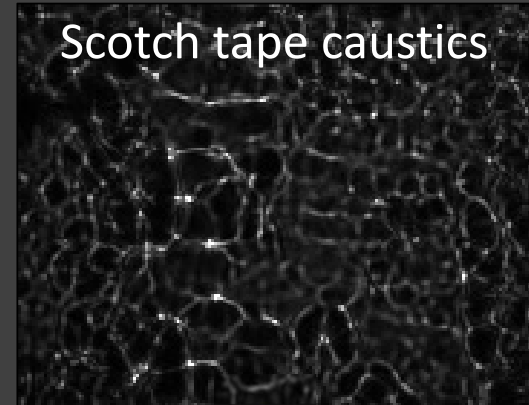


+



=

Scotch tape caustics



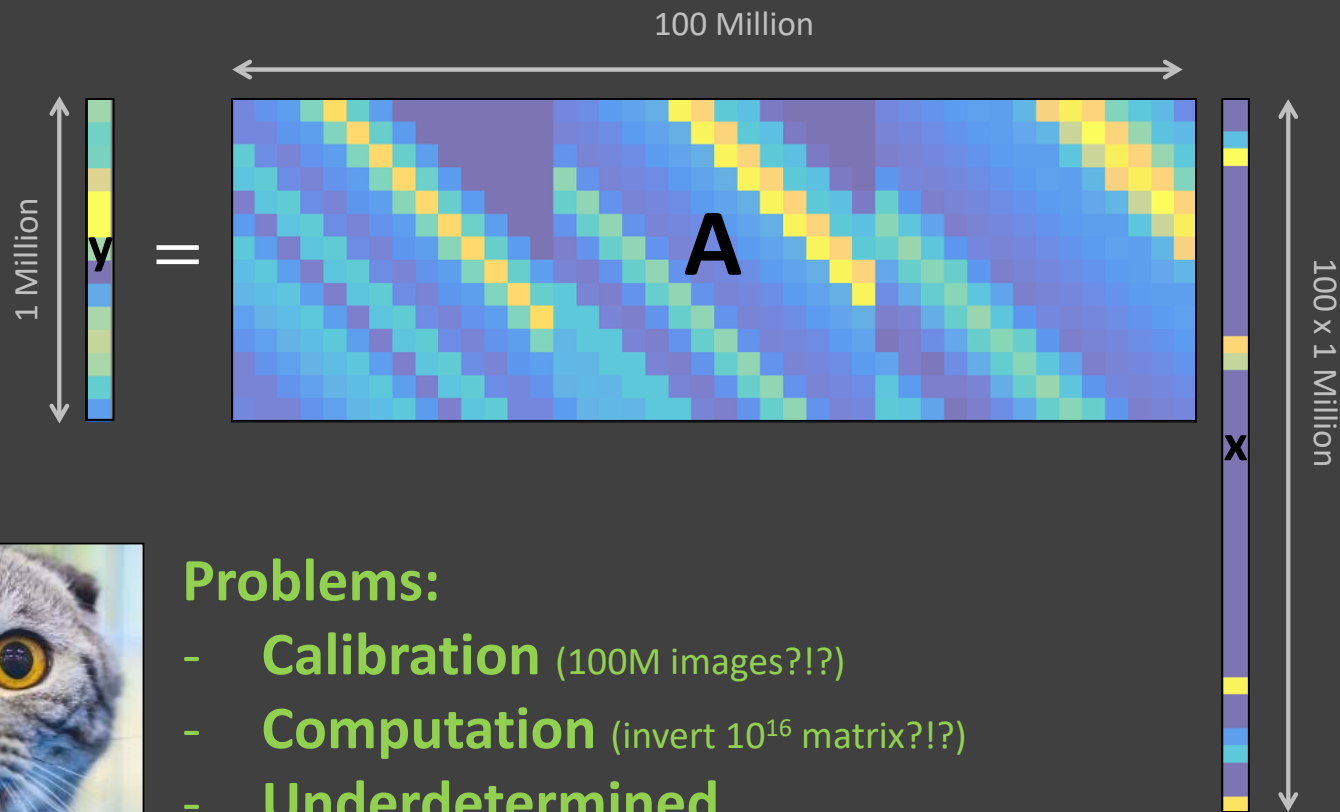
Reconstruction



Camille Biscarrat
Shreyas Parthasarathy

2D $\Rightarrow$ 3D

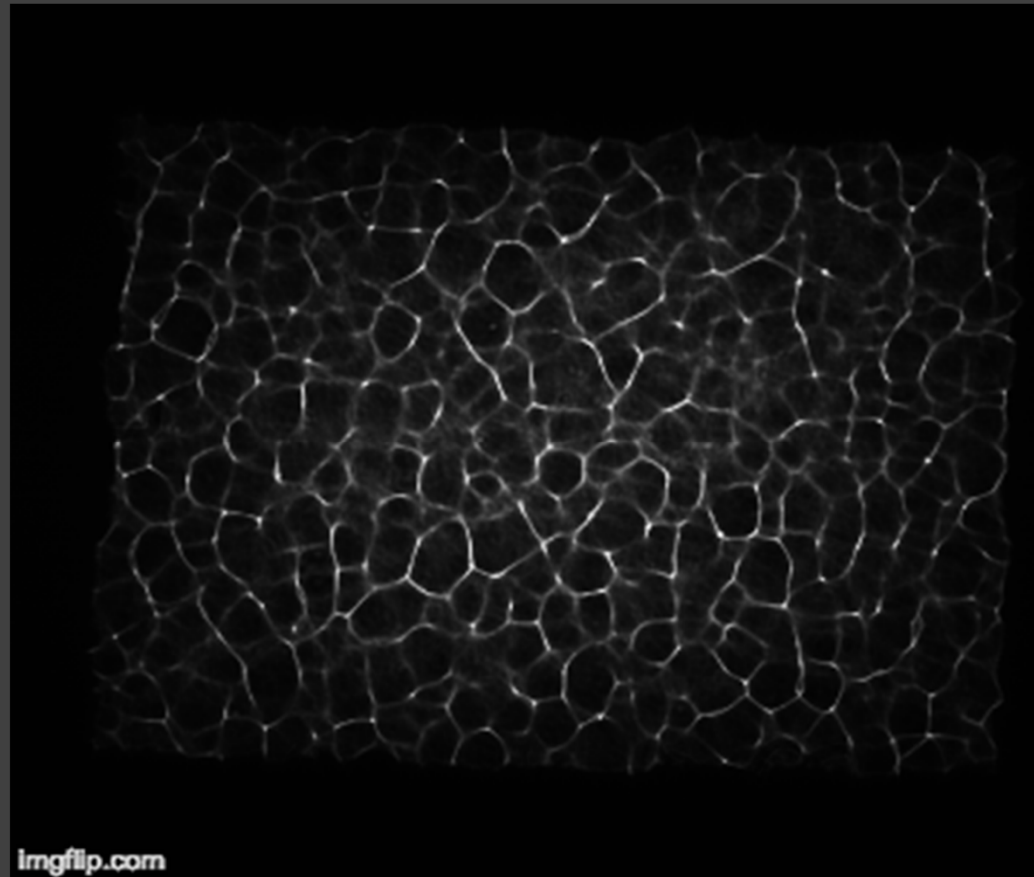
3D is not so easy



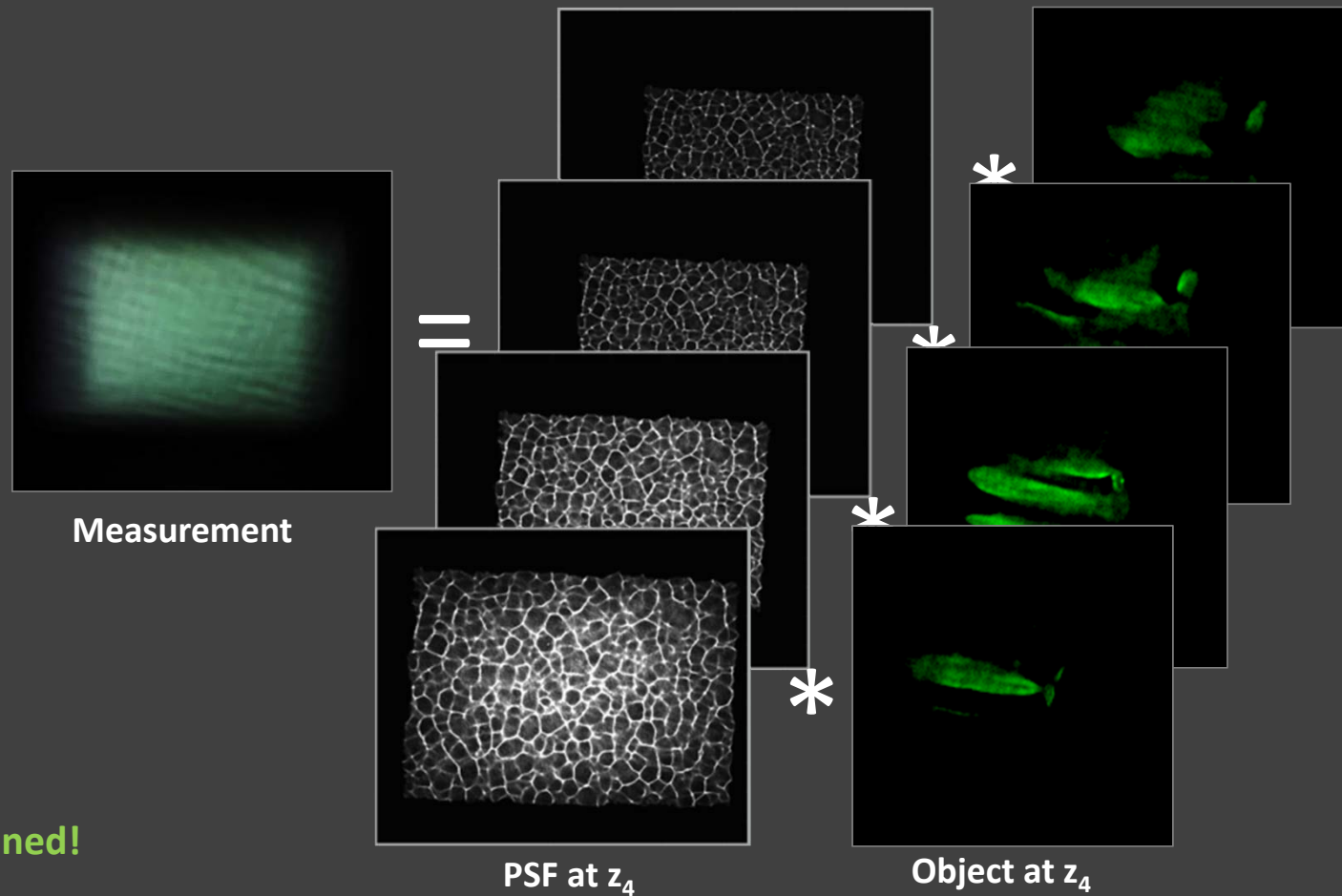
Problems:

- **Calibration** (100M images?!?)
- **Computation** (invert 10^{16} matrix?!?)
- **Underdetermined**

The PSF scales with depth

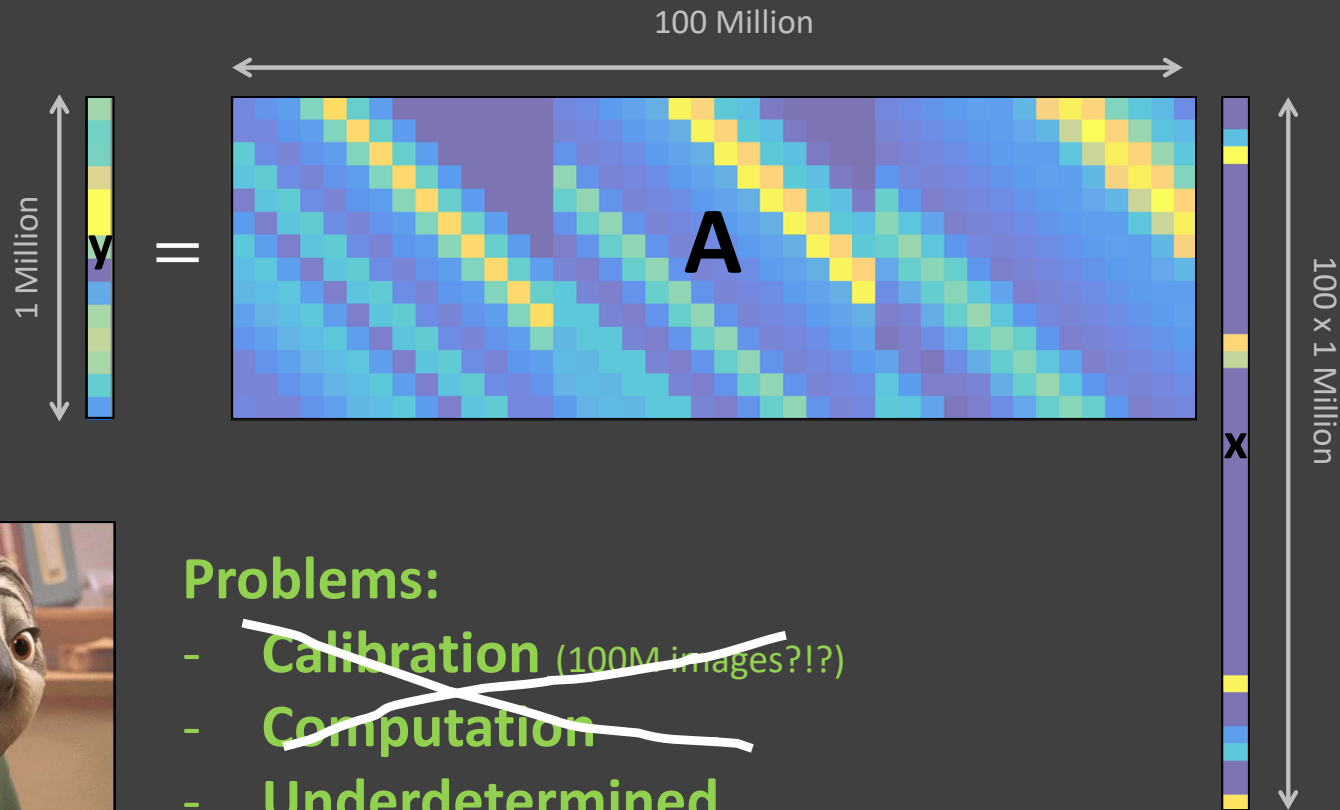


3D forward model is a sum of convolutions



very
underdetermined!

3D is not so easy



Problems:

- ~~Calibration~~ (100M images?!?)
- ~~Computation~~
- Underdetermined

Compressed sensing to the rescue!

solves under-determined problems via a sparsity prior

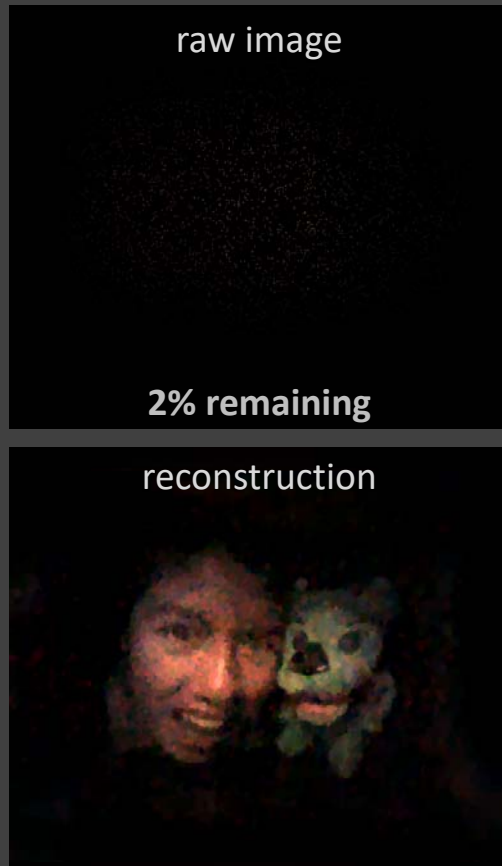


Image Reconstruction with Sparsity Prior

$$\begin{aligned}
 & \arg \min_{\substack{\text{stack of images} \\ \geq 0}} \left\| \begin{array}{c} \text{stack of images} \\ \text{stack of images} \end{array} \right\|_2^2 \\
 & + \lambda \left\| \begin{array}{c} \text{stack of images} \\ \text{stack of images} \end{array} \right\|_{TV} \\
 & \text{Sparsity basis}
 \end{aligned}$$

Diagram illustrating the image reconstruction problem with a sparsity prior. The objective function is the sum of two terms:

- The first term is the squared L2 norm of the difference between the observed data y (a stack of images) and the reconstruction Ax (the product of a sparsity basis A and the unknown image x).
- The second term is the L1 norm (Total Variation, TV) of the reconstructed image x , weighted by the regularization parameter λ .

The sparsity basis A is represented by a stack of images, and the unknown image x is also represented by a stack of images.

***solved with ADMM in Halide**

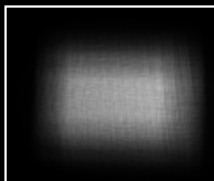
S. Boyd, et al. *Foundations and Trends in Machine Learning* (2011)

J. Ragan-Kelley, et al. *AMC SIGPLAN* (2013)

EDMUND

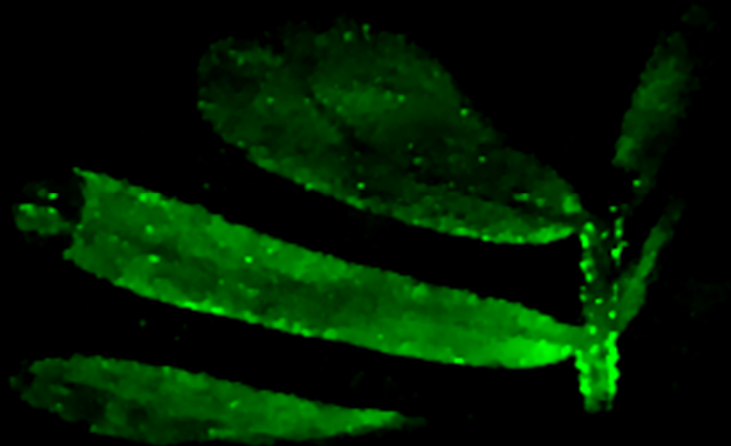
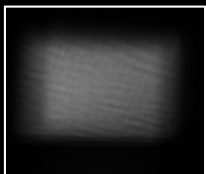


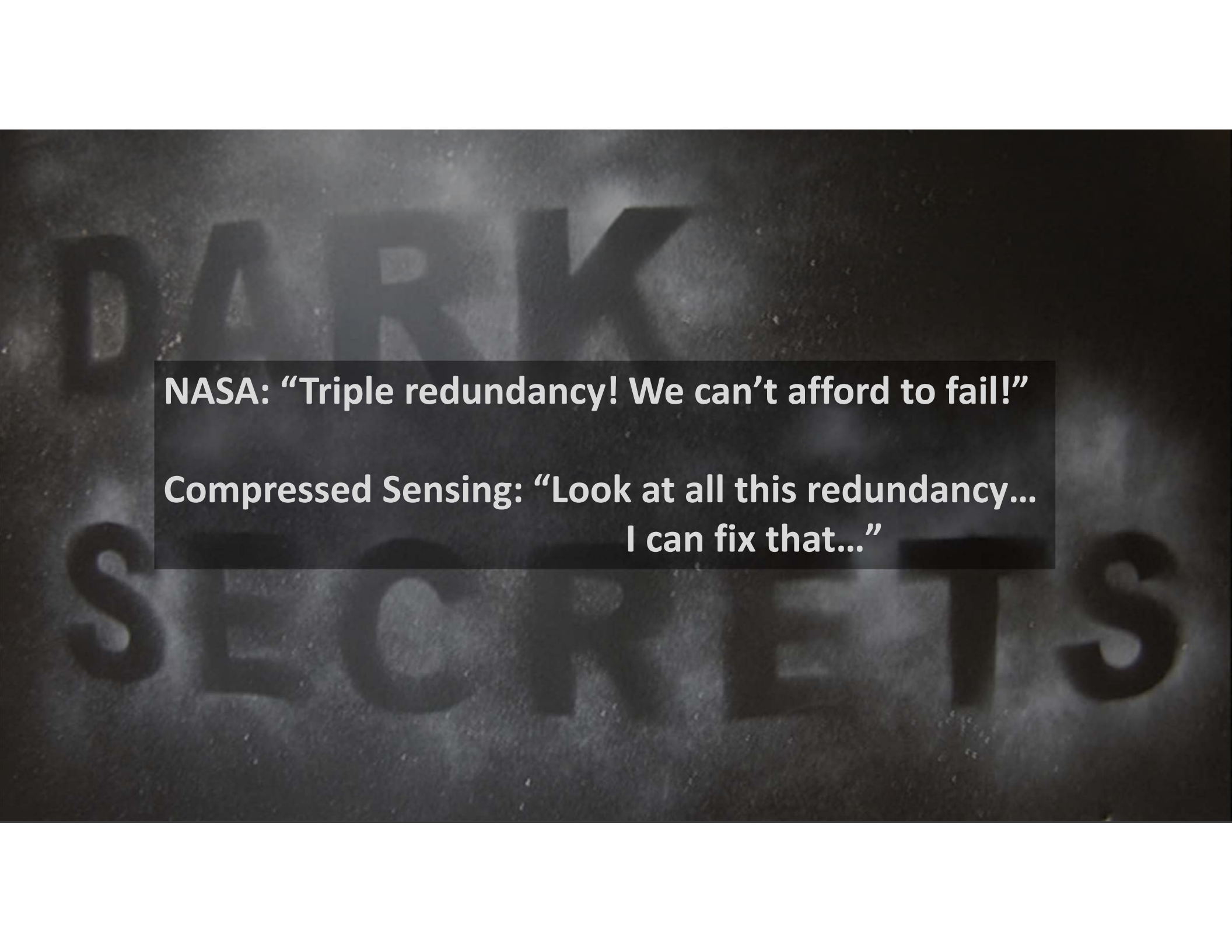
USAF 1951 1X



$z = 16.14 \text{ mm}$

536 million voxels
(cropped to 39 million)

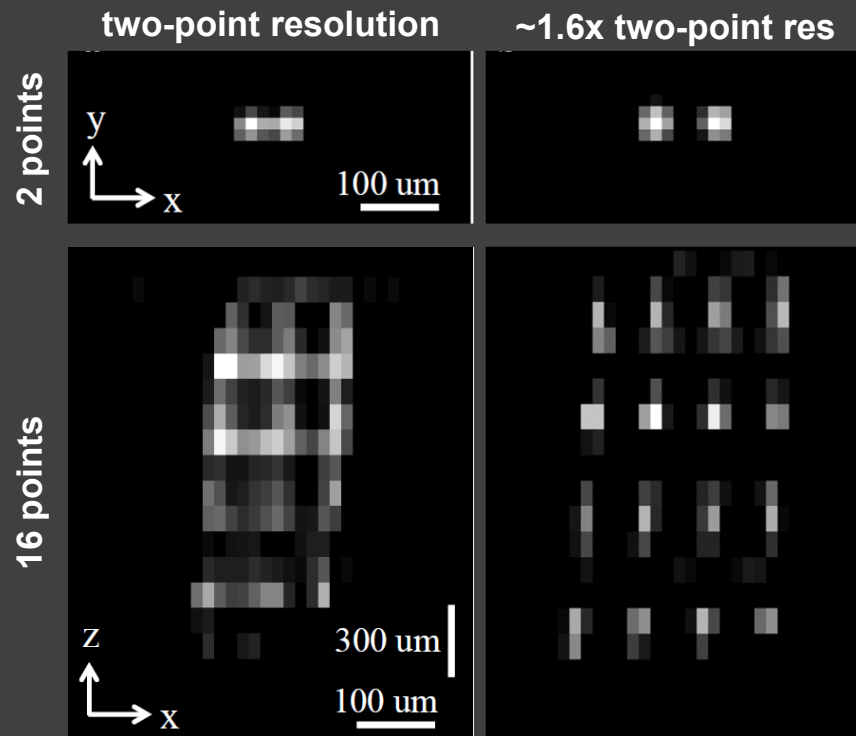




NASA: “Triple redundancy! We can’t afford to fail!”

**Compressed Sensing: “Look at all this redundancy...
I can fix that...”**

Challenge: object-dependent resolution



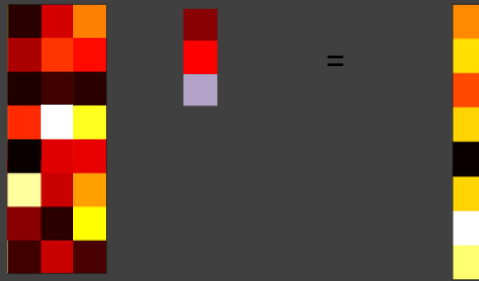
*Two-point resolution only predicts **best case** scenario.*

Solution?: use condition number of sub-problem

Assume we know where non-zero elements are:

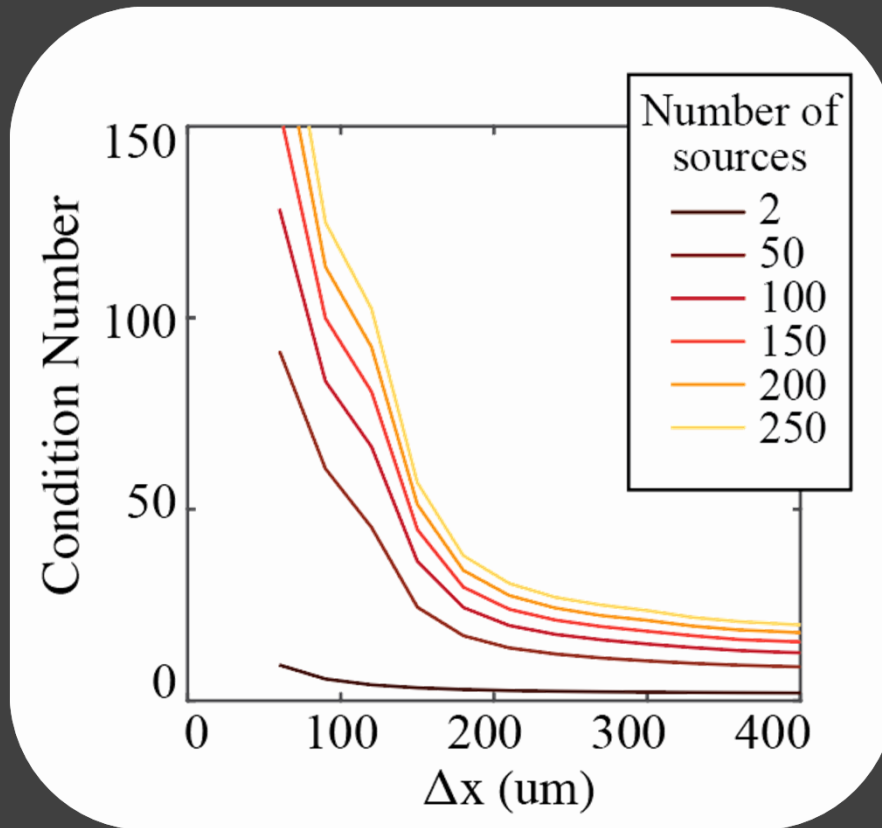


Solution?: use condition number of sub-problem

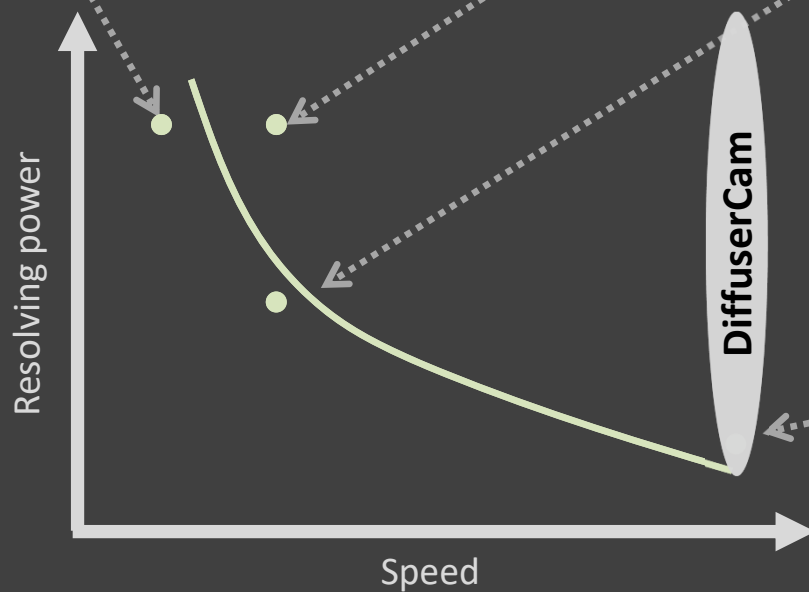
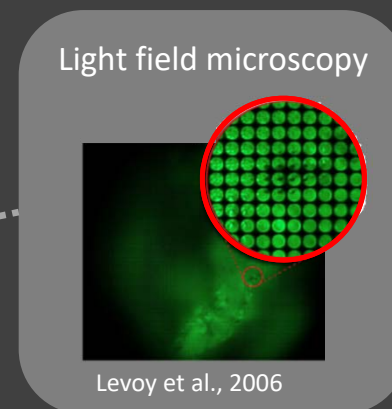
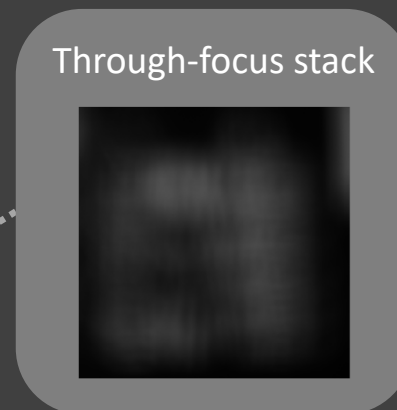
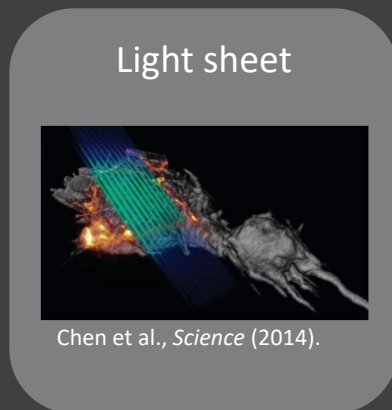


Now it is a small least squares problem

Solution?: use condition number of sub-problem



Local condition number sort of gives worst case scenario



**Scanning
Microscopy**



**speed scales with #
voxels in image**

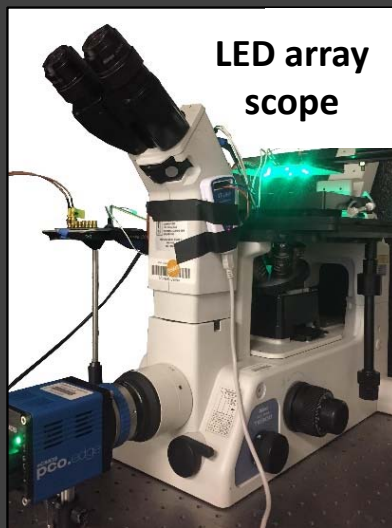
vs.

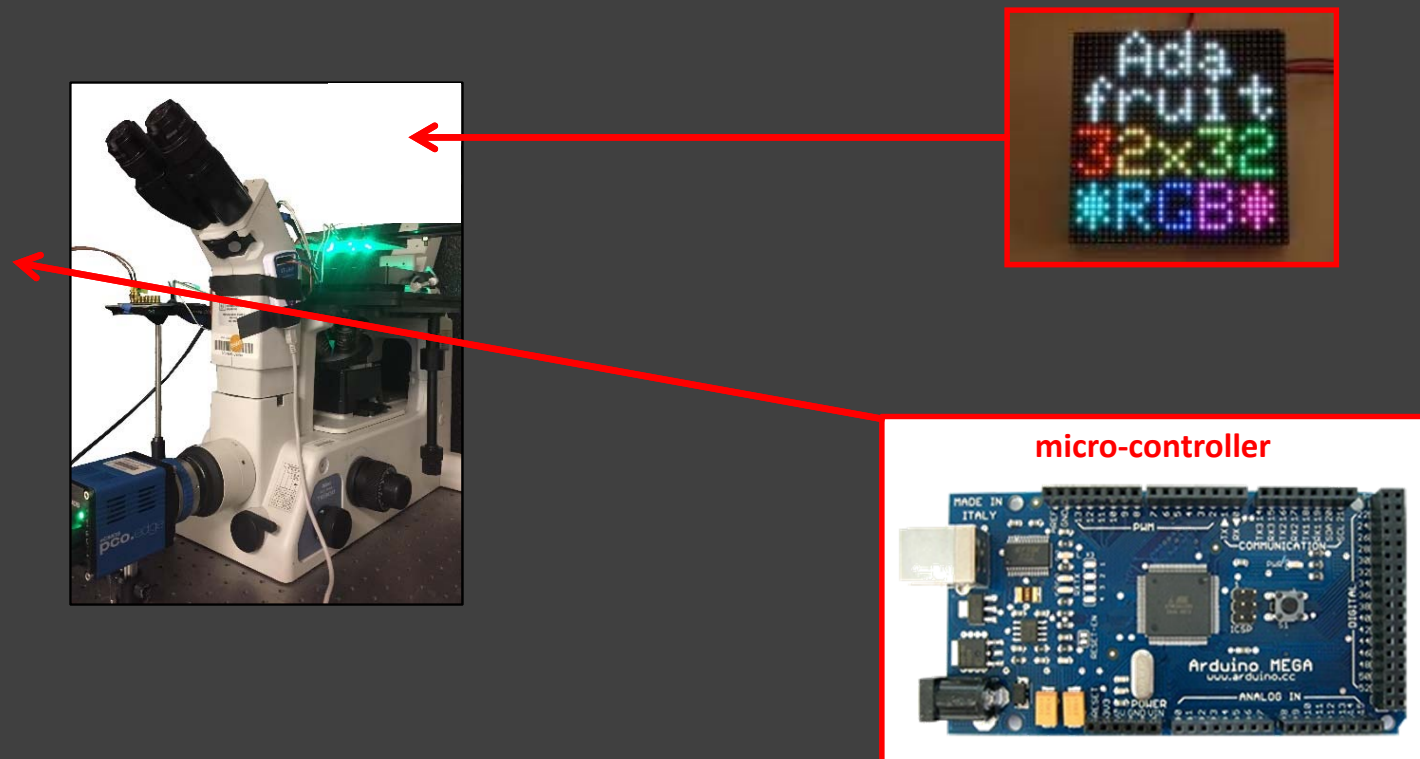
**Compressed
Sensing**

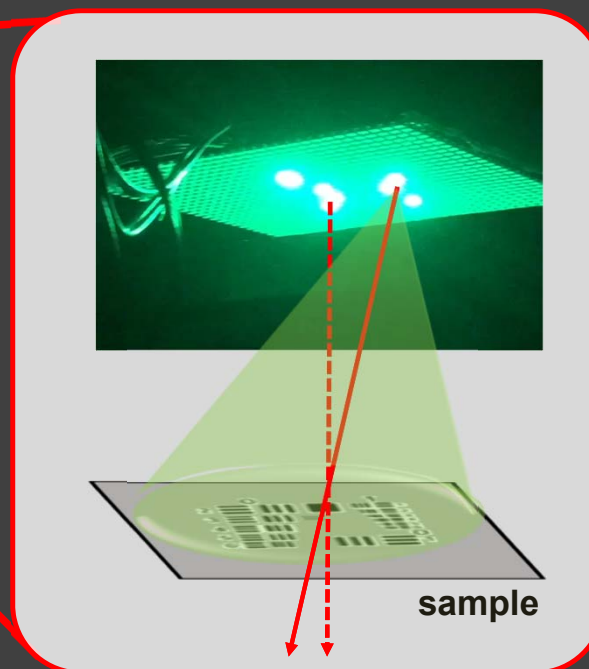
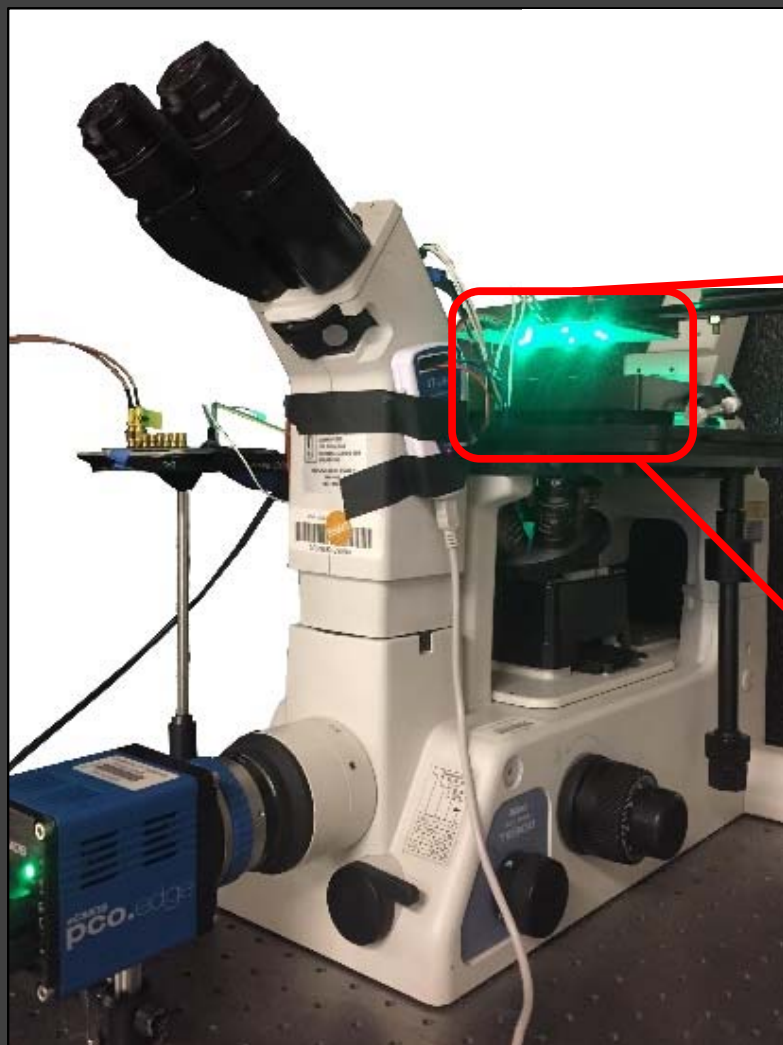


**speed scales with
sparsity of sample**

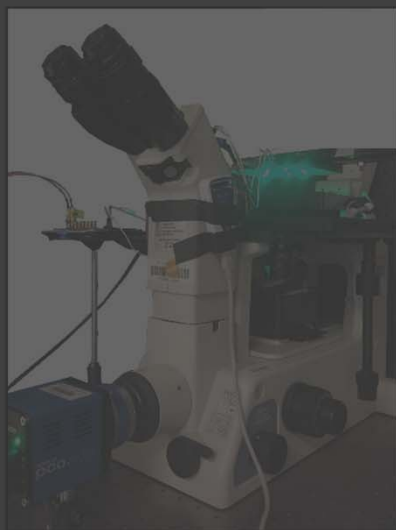
This talk:



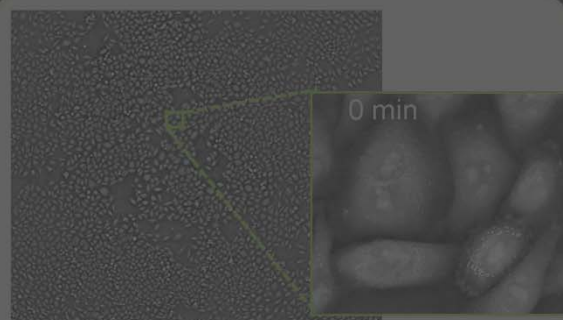
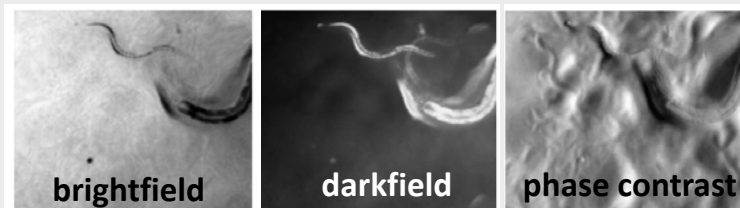




LEDs pattern illumination angles



Real-time multi-contrast



Gigapixel imaging

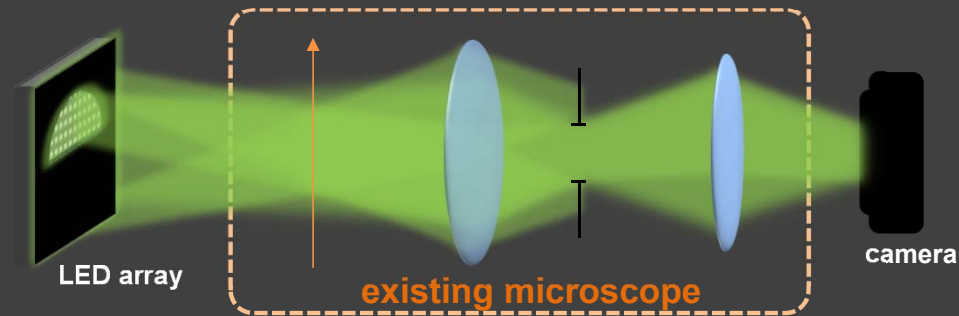
3D
imaging



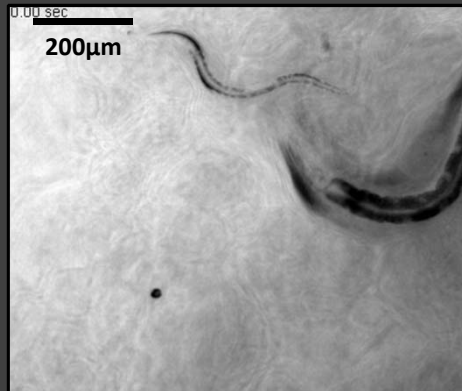
**darkfield means
indirect illumination**



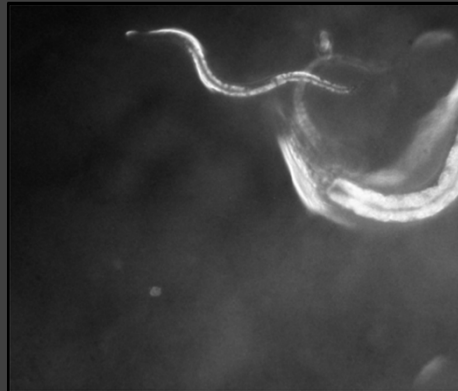
Multi-contrast with an LED array microscope



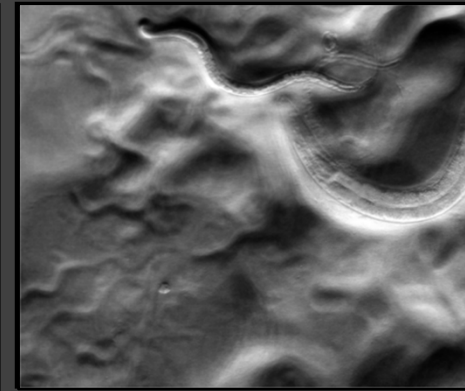
brightfield



darkfield^[1]

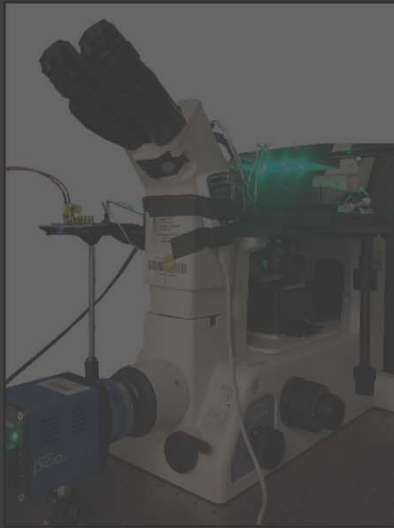


phase contrast^[2]

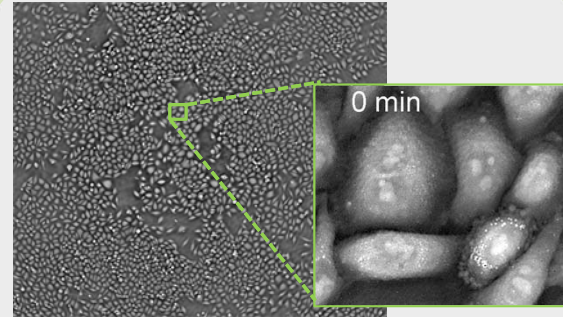


[1] G. Zheng, C. Kolner, C. Yang, *Opt. Lett.*, (2011).

[2] L. Tian, J. Wang, L. Waller, *Opt. Lett.* (2014).

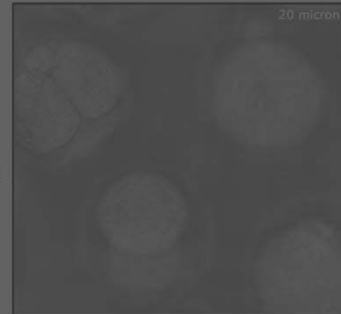


Real-time multi-contrast

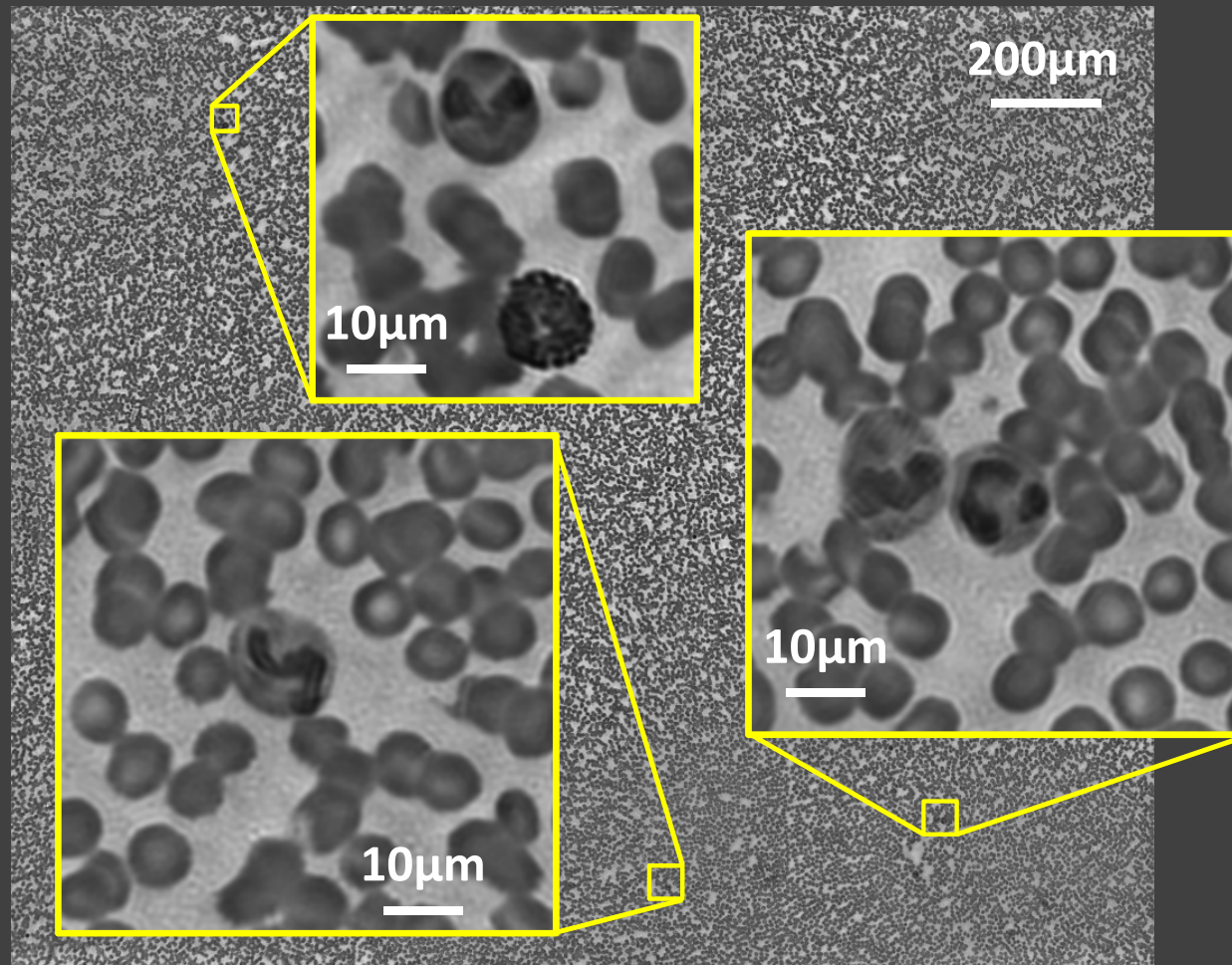


Gigapixel imaging

3D imaging



Gigapixel imaging for disease screening

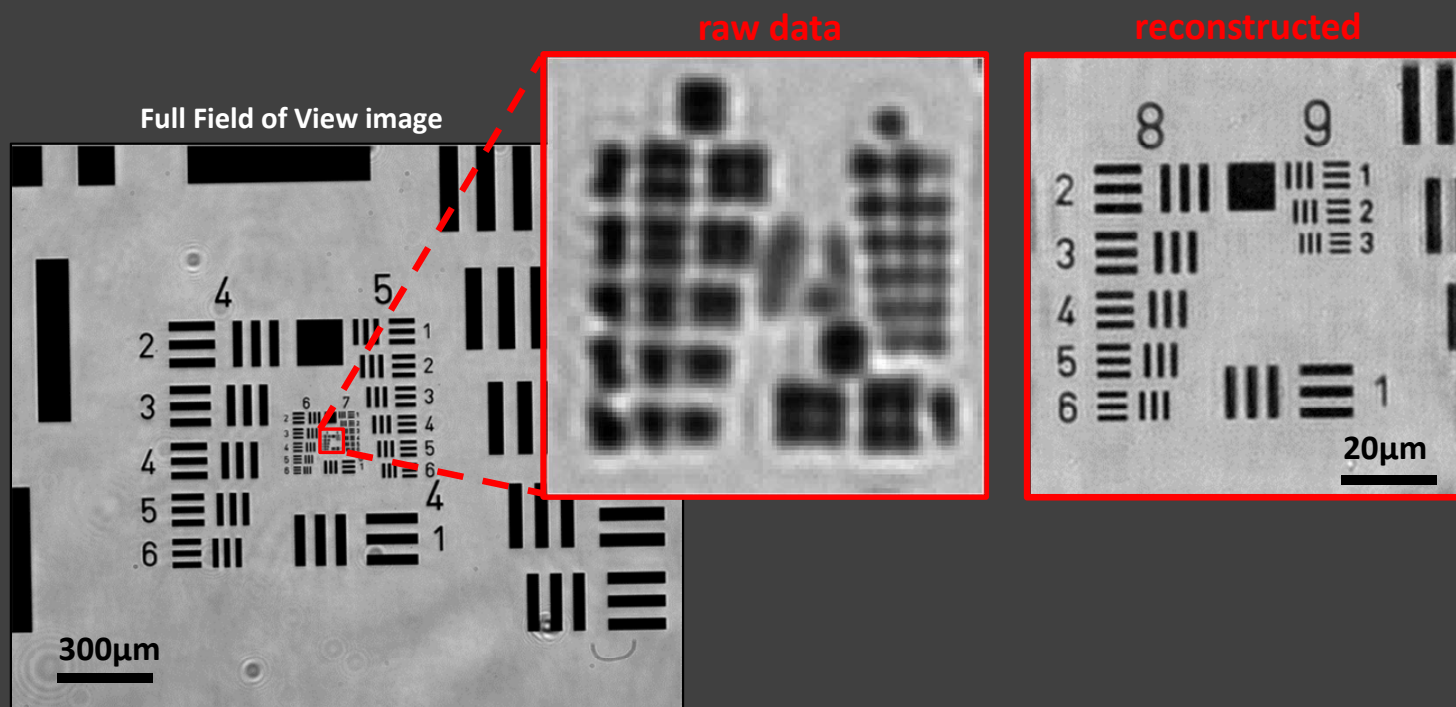


Stained Human
Blood Cells
FoV~2.1mmx1.7mm
resolution ~0.4µm

26k x 22k pixels

G.Zheng, R. Horstmeyer, C. Yang, *Nat. Photon.* (2013).
L.Tian, X.Li, K.Ramchandran, L. Waller, *Biomed. Opt. Express* (2014).

Super-resolution from coded illumination

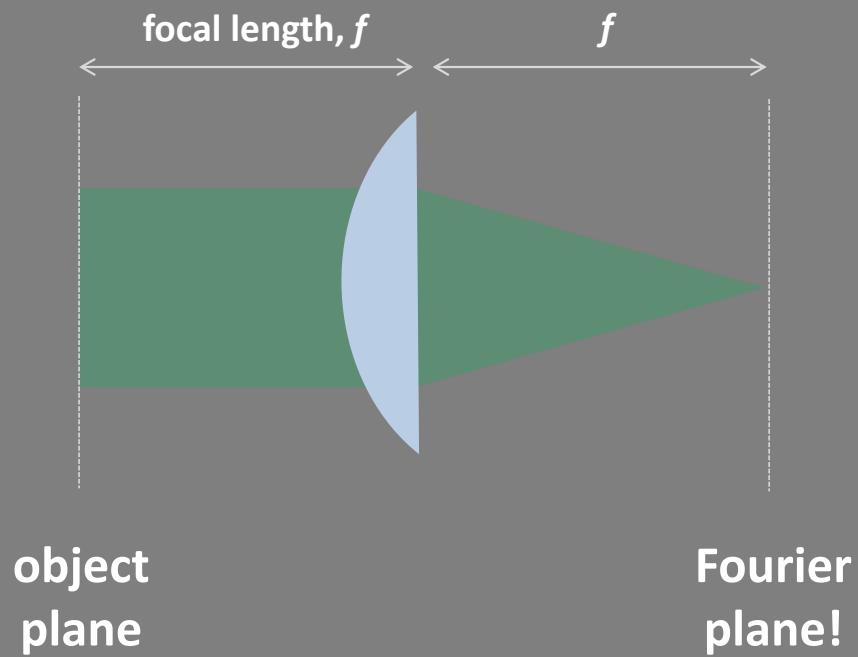


G.Zheng, R. Horstmeyer, C. Yang, *Nat. Photon.* (2013).

L.Tian, X.Li, K.Ramchandran, L. Waller, *Biomed. Opt. Express* (2014).



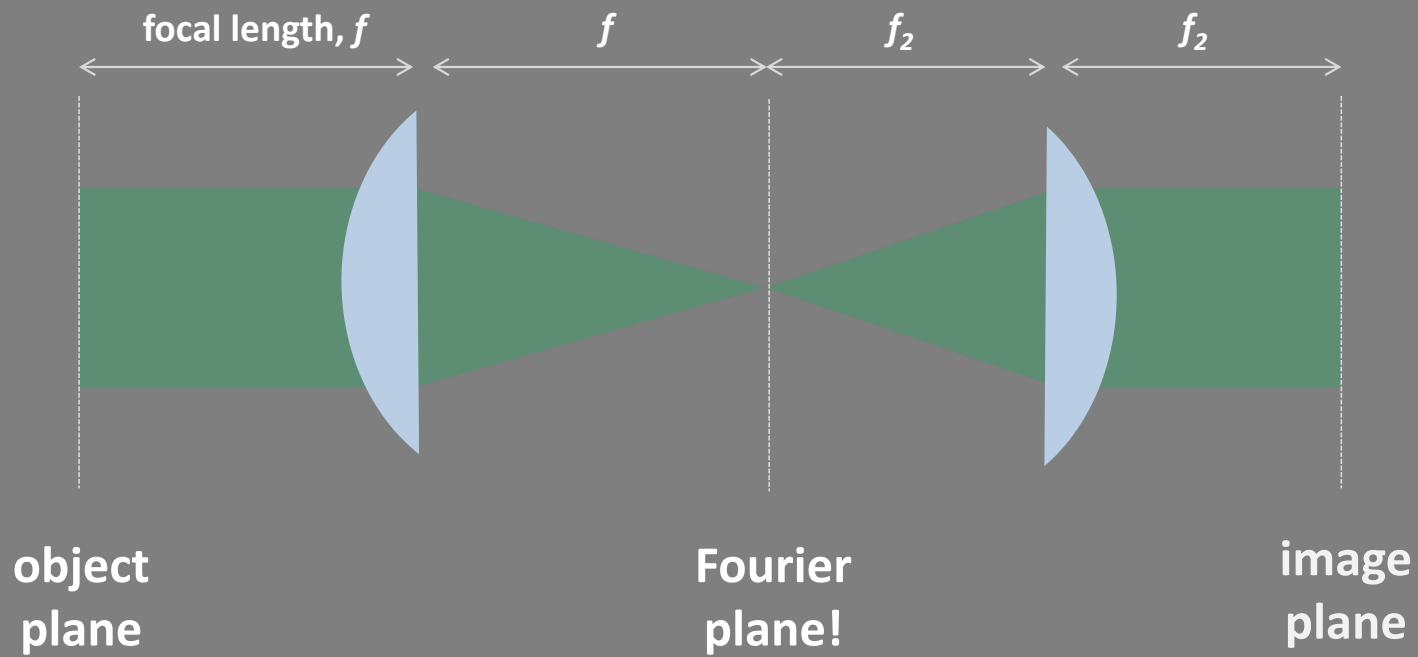
A lens can perform a Fourier transform!



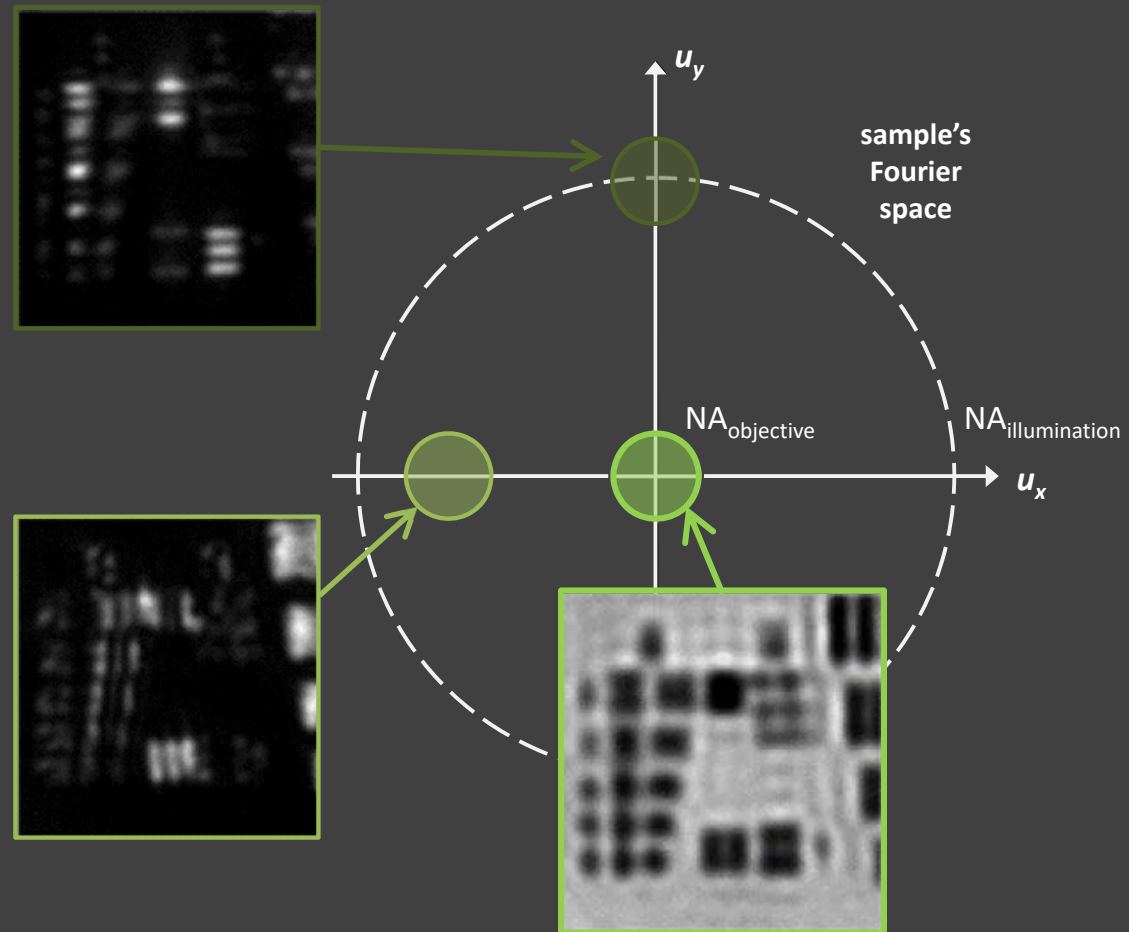
DETOUR



A microscope does TWO Fourier transforms!



Synthetic aperture: filling in frequency space



Our version of ideas in:
G. Zheng, R. Horstmeyer, C. Yang, *Nat. Photon.* (2013).

Fourier Ptychography: synthetic aperture + phase retrieval

Forward model:

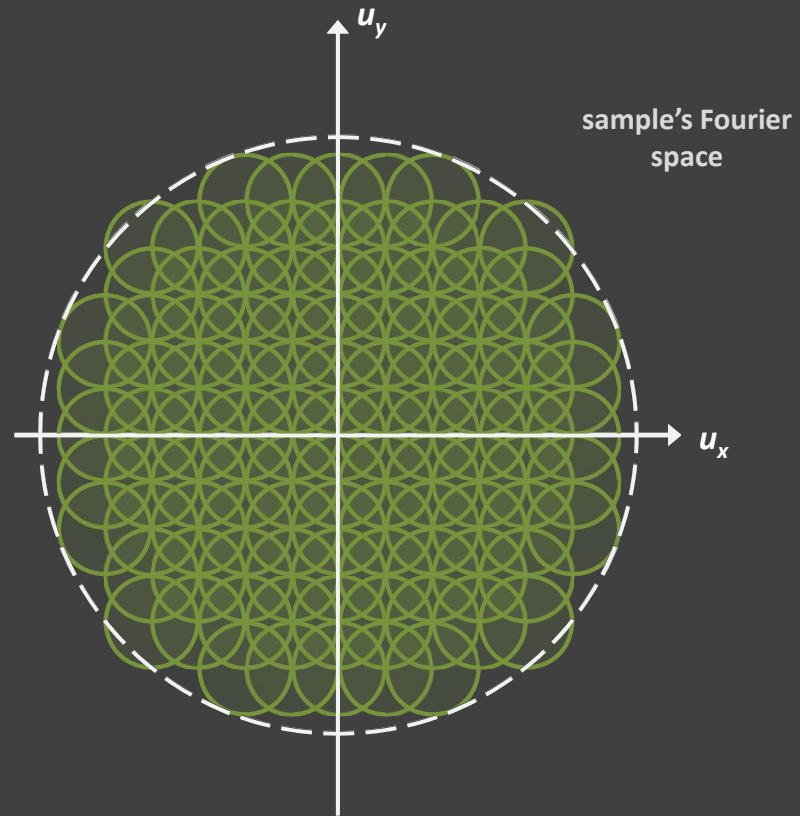
$$\mathbf{y} = |\mathbf{Ax}|^2$$

measurements system matrix object

Inverse problem:

$$\min_{\mathbf{O}(\mathbf{u})} \sum_n \sum_r \left| \mathbf{I}_n(\mathbf{r}) - \left| \mathfrak{F}^{-1} \{ \mathbf{O}(\mathbf{u} - \mathbf{u}_n) \cdot \mathbf{P}(\mathbf{u}) \} \right|^2 \right|^2$$

Solve for me! And me!

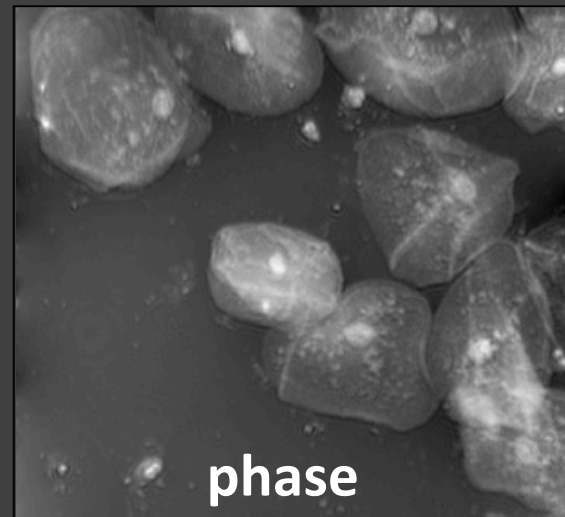
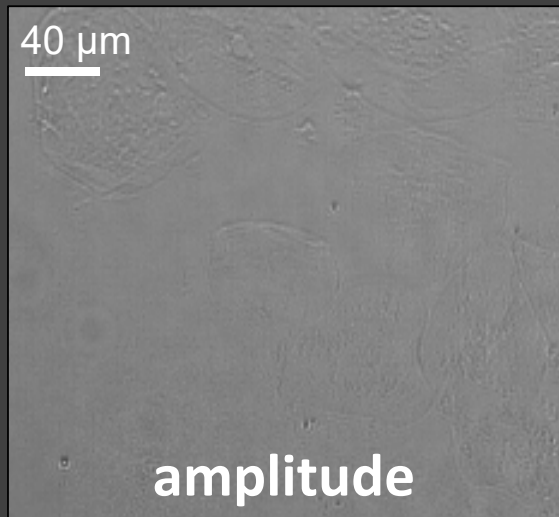


J. Rodenburg, H. Faulkner, *Appl. Phys. Lett.* 85 (2004).
 M. Guizar-Sicairos, J. Fienup, *Opt. Express* 16 (2008).
 L. Tian, X. Li, K. Ramchandran, L. Waller, *Biomed. Opt. Express* (2014).
 S. Alexandrov, T. Hillman, T. Gutzler, D. Sampson, *Phys. Rev. Lett.* 97 (2006).

A. Kirkland, et al., *Ultramicroscopy* 57 (1995).
 G. Zheng, R. Horstmeyer, C. Yang, *Nat. Photon.* (2013).
 O. Xu, C. Yang, *Opt. Express* (2013).
 P. Thibault, et al., *Ultramicroscopy* 109 (2009).
 T. Hillman et al., *Opt. Express* (2009).

Computational ^{Phase} imaging

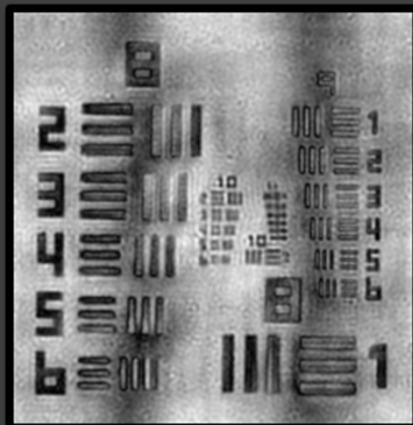
phase imaging *must* be computational



We can only measure intensity $y = |\mathbf{Ax}|^2$

2nd order optimization is better

1st order
(Gradient descent)



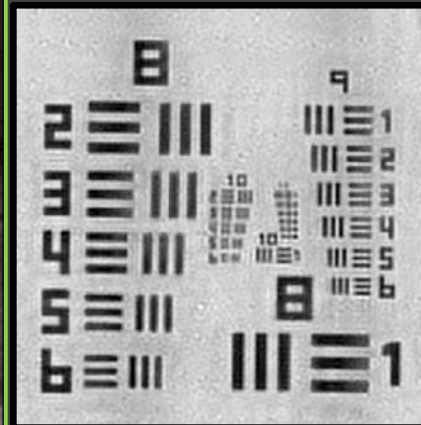
3 seconds

quasi 2nd order

speed vs. accuracy



2nd order
(Newton)

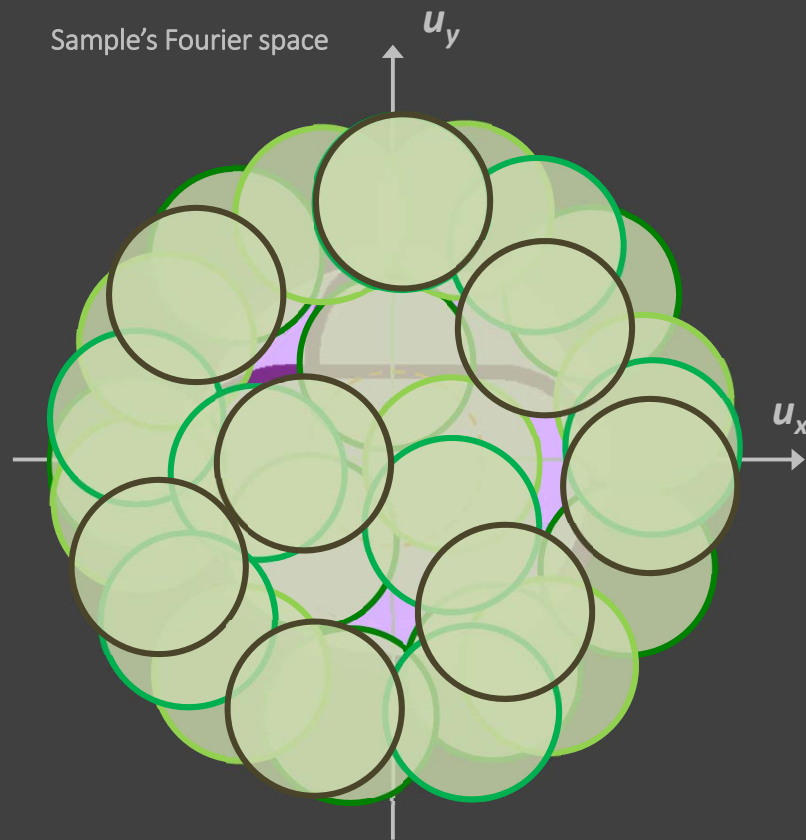


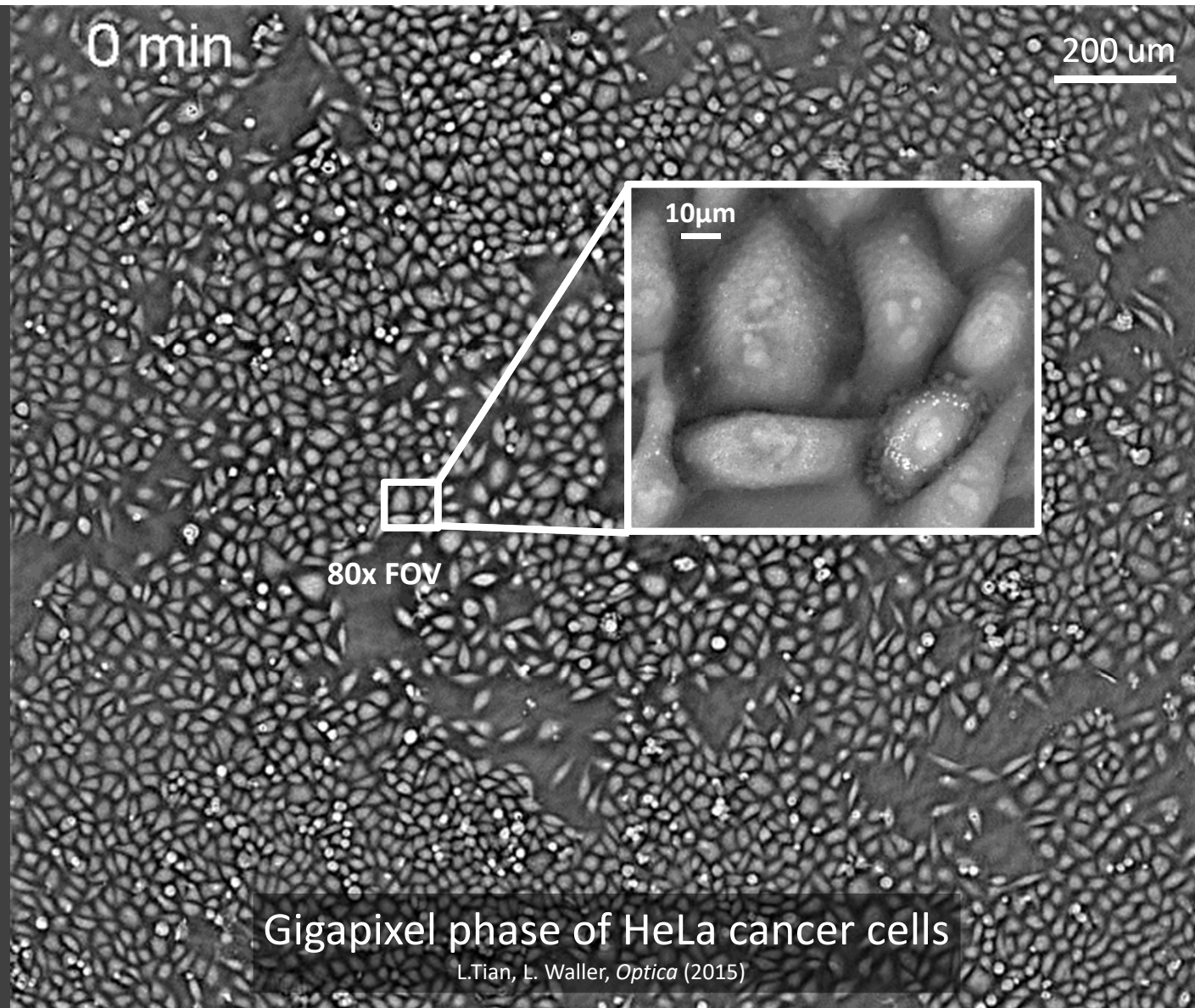
100 seconds

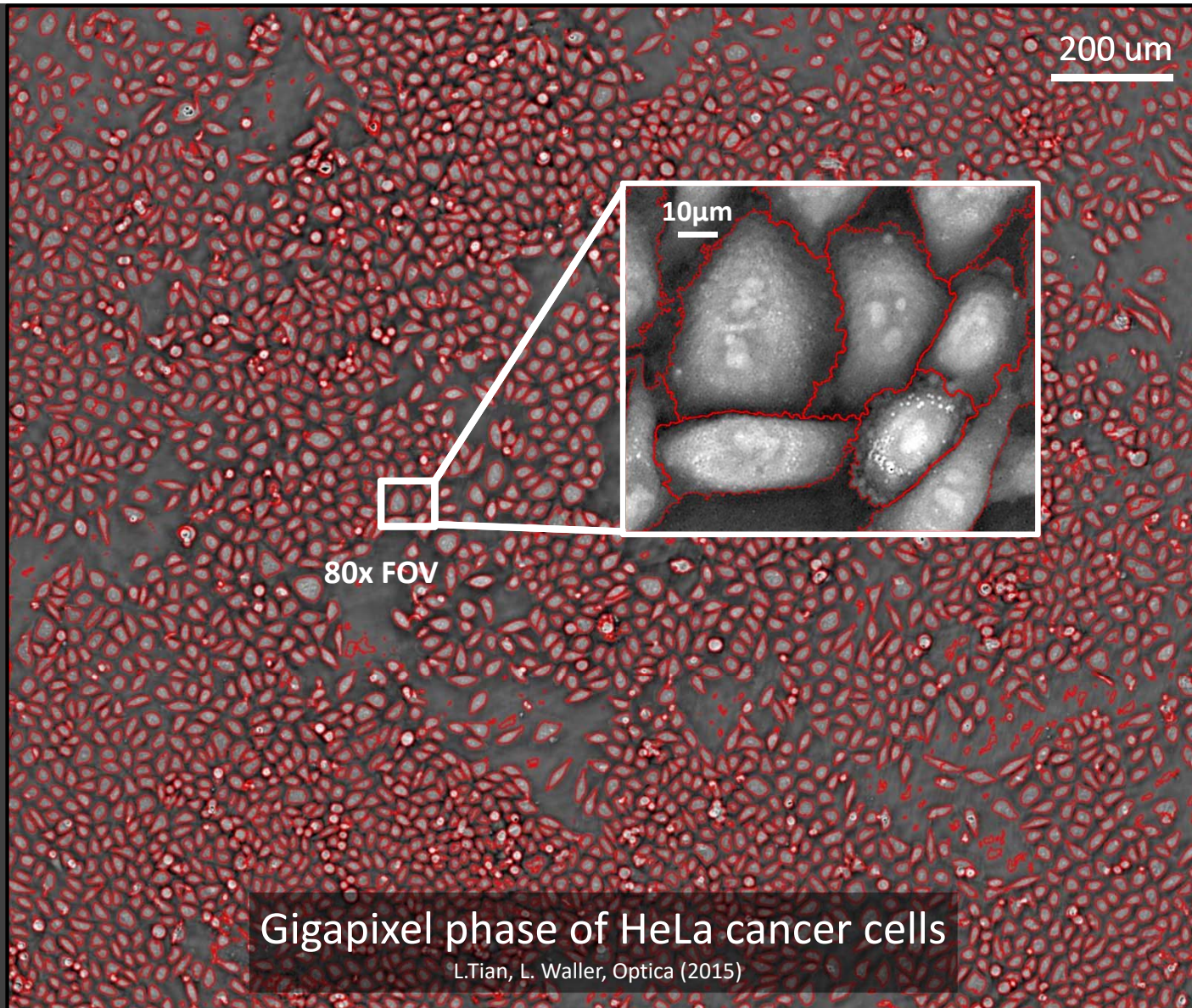
Li-Hao Yeh



Designer illumination codes for fast acquisition







Segmentation by
CellProfiler

DARK

SECRETS

Recipe for computational imaging

$$y = Ax$$

1 Physics

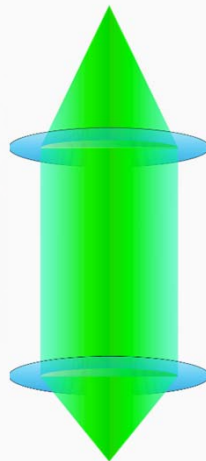
$$\nabla \cdot \mathbf{D} = \rho_v$$

$$\nabla \cdot \mathbf{B} = 0$$

$$\nabla \times \mathbf{E} = -\frac{\partial \mathbf{B}}{\partial t}$$

$$\nabla \times \mathbf{H} = \frac{\partial \mathbf{D}}{\partial t} + \mathbf{J}$$

2 Optical Design



3 CALIBRATION





Laura's Law:

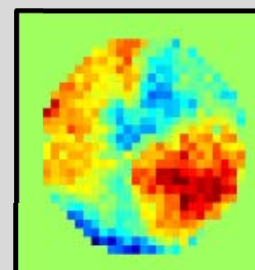
$$\text{Reproducibility} \propto \frac{1}{\text{\# of critical pieces of duct tape}}$$

Algorithmic self-calibration

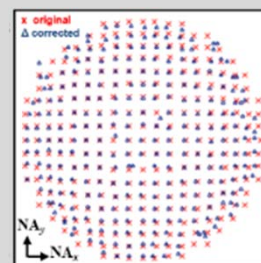
$$\mathbf{y} = |\mathbf{Ax}|^2$$

measurements $\mathbf{y}$
 system matrix $\mathbf{A}$
 object $\mathbf{x}$

Experimental errors:

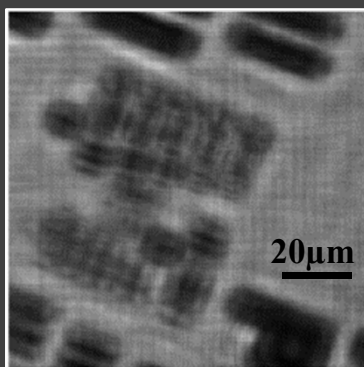


Aberrations

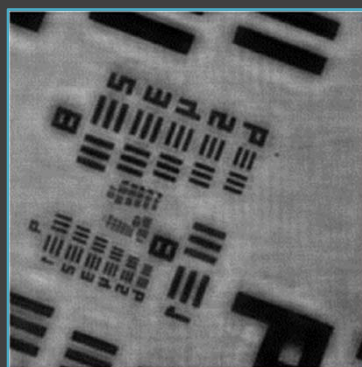


LED positions

not calibrated



calibrated



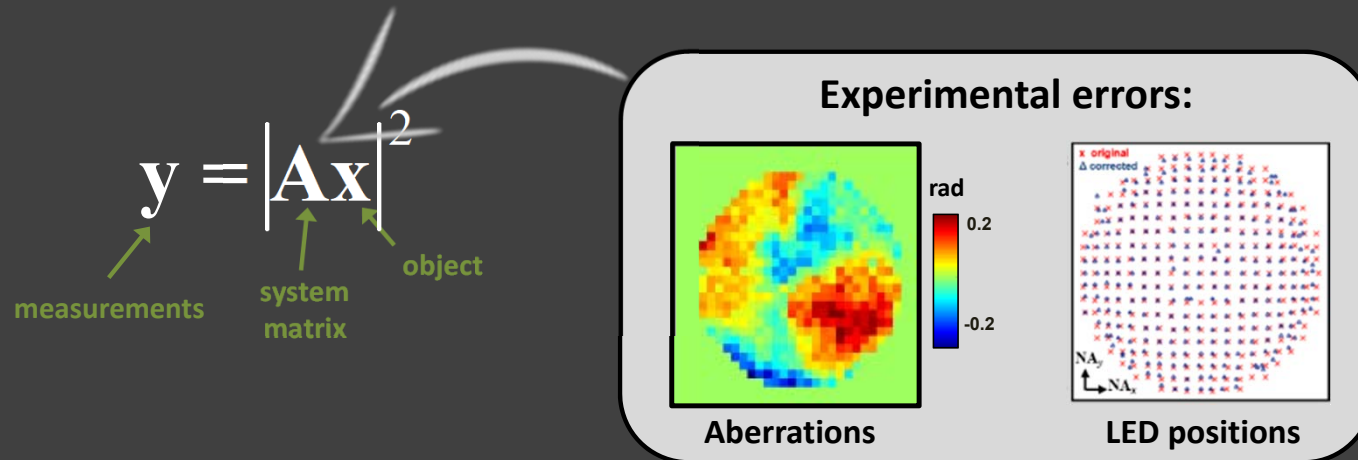
$$\mathbf{A} \rightarrow \mathbf{A}(\boldsymbol{\theta})$$

calibration parameters $\boldsymbol{\theta}$

Regina
Eckert



Algorithmic self-calibration



I don't wanna calibrate anymore!

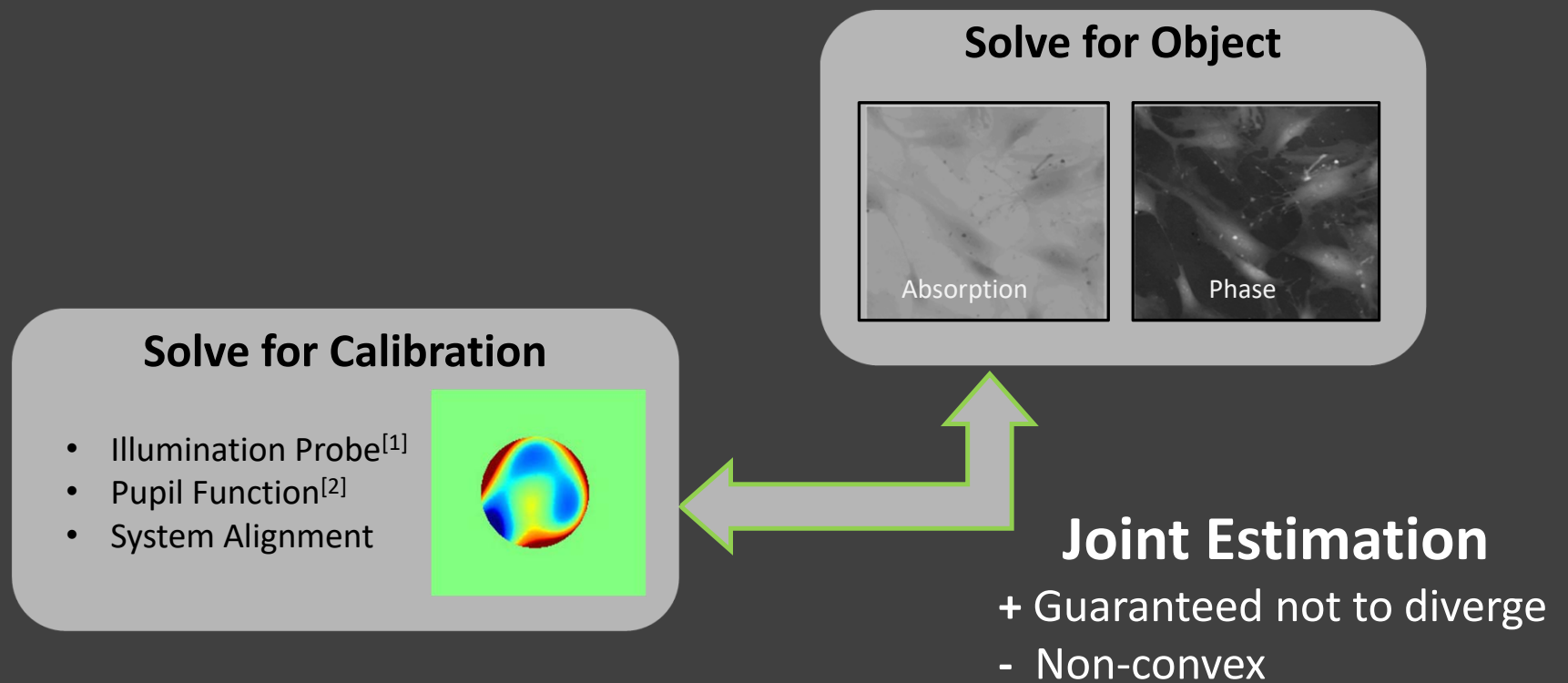
$$\min_{\mathbf{x}, \boldsymbol{\theta}} \left\| \mathbf{y} - \mathbf{A}(\boldsymbol{\theta}) \mathbf{x} \right\| + \lambda_1 \|\mathbf{x}\|_1 + \lambda_2 \|\boldsymbol{\theta}\|_2$$

calibration parameters

Regina Eckert



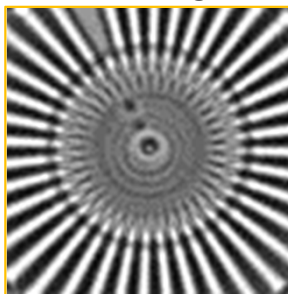
If it's critical, then let's design around it!



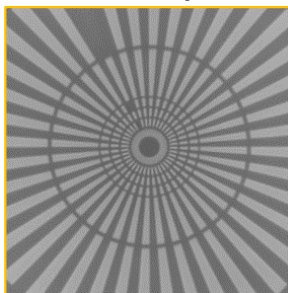
[1] M. Guizar-Sicairos and Fienup J. R. Opt. Exp. (2008) [2] X. Ou et al., Opt Exp. (2014).

200 μm

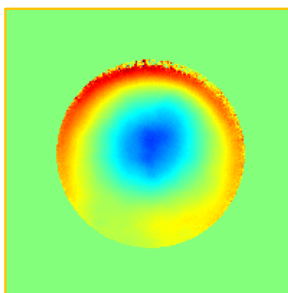
raw image



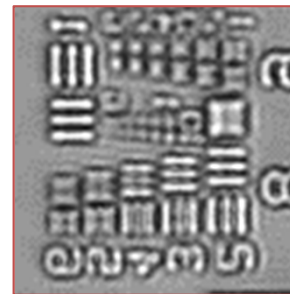
recovered phase



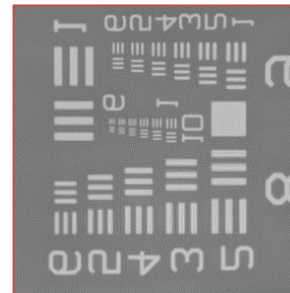
aberrations



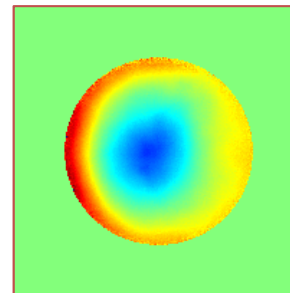
raw image

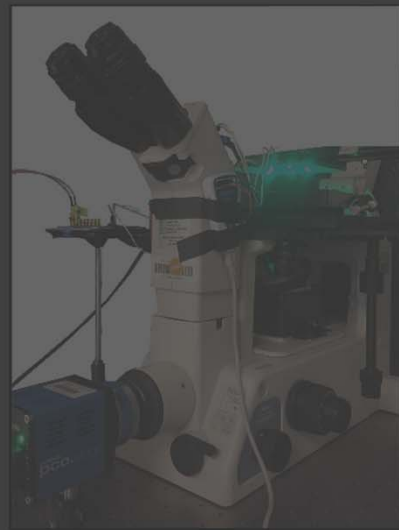


recovered phase



aberrations

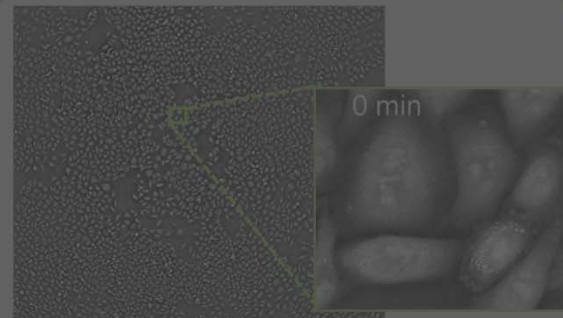




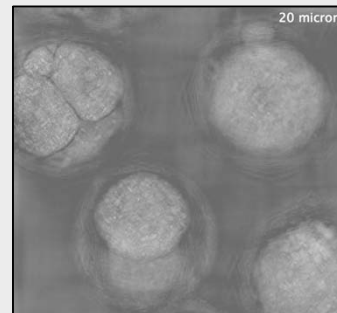
Real-time multi-contrast



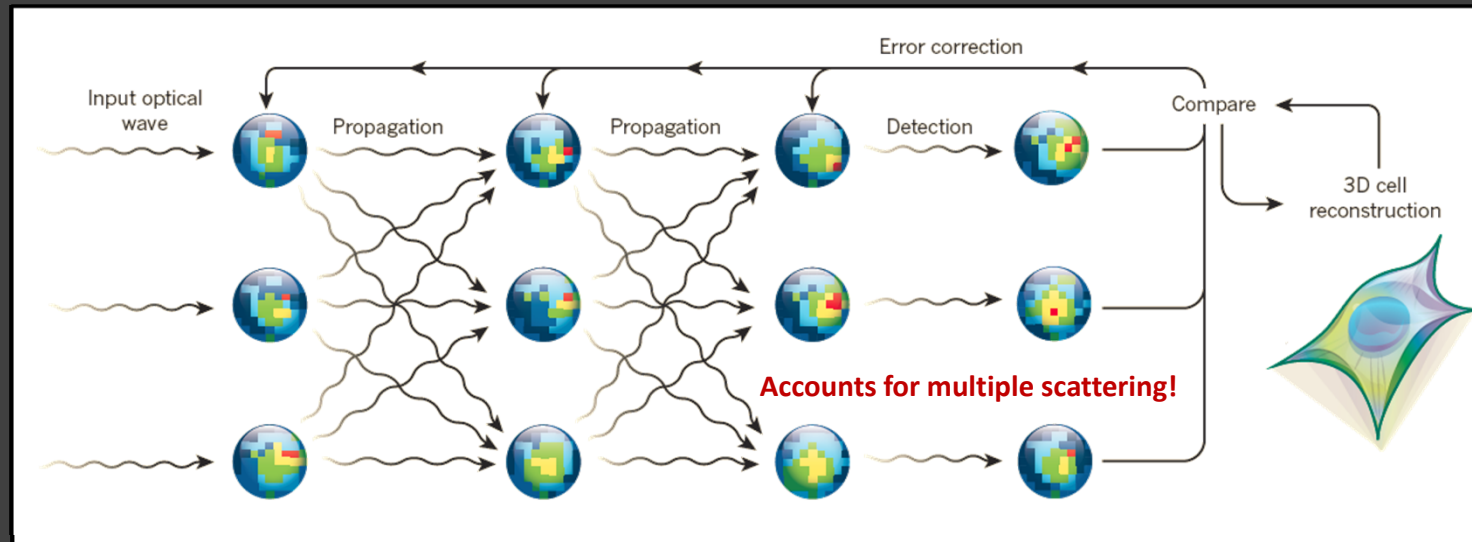
Gigapixel imaging



**3D
imaging**



3D phase imaging as a neural network

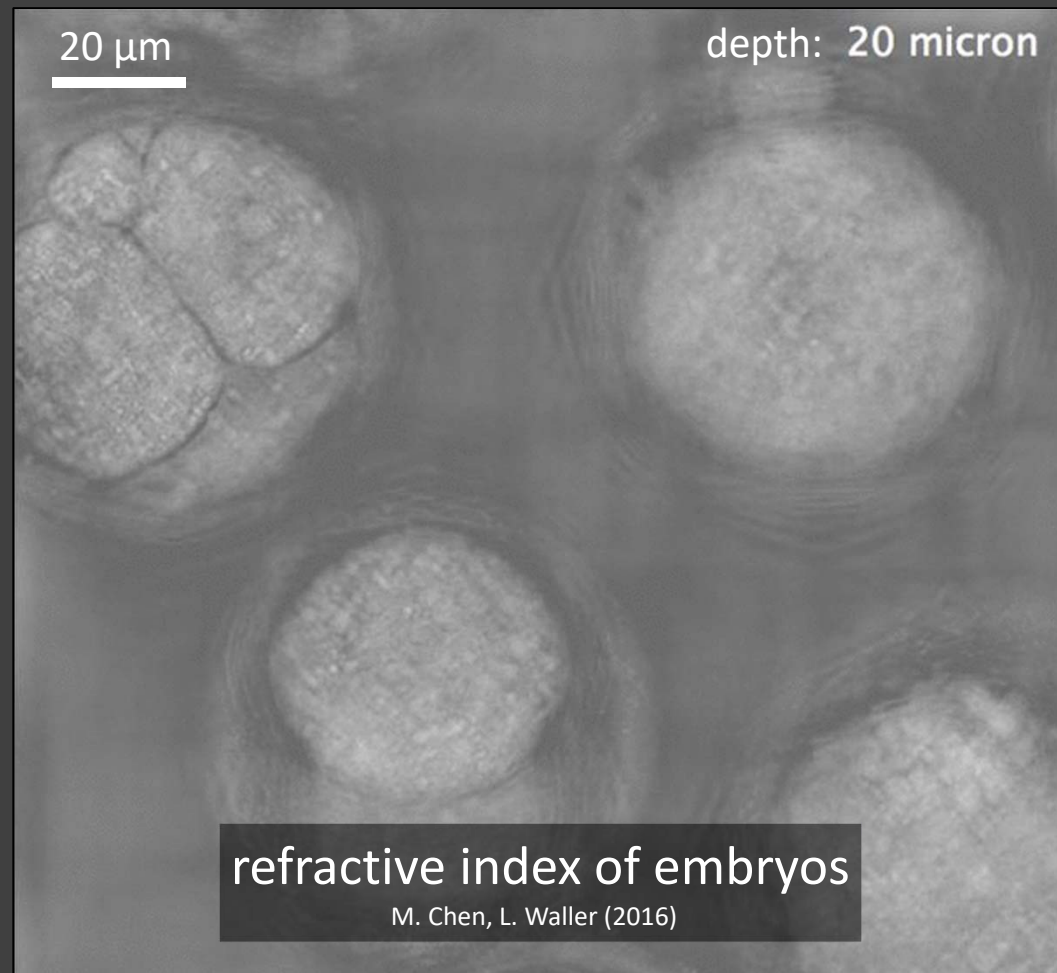


Nonlinear, nonconvex...
so will it converge?

Van Roey, van der Donk, Lagasse, *J. Opt. Soc. Am.* (1981)
Cowley, Moodie, *Acta Crystallogr.* (1957).
Maiden, Humphry, Rodenburg, *J. Opt. Soc. Am. A* (2012).
Tian, Waller, *Optica* (2015)
Van den Broek, Koch, *Phys. Rev. Lett.* (2012)
Van den Broek, Koch, *Phys. Rev. B* (2013)
Kamilov, Papadopoulos..., Psaltis, *Optica* (2015)
Waller, Tian, *Nature* (2015).

Analogy to Artificial Neural Networks

3D refractive index measurement



Michael
Chen

Outlook

Hardware Toolbox



Computational Toolbox



Computers + Optics should talk more!

Collaborators:

Hillel Adesnik (Neuro)
Ben Recht, Ren Ng (EECS)
David Schaffer, Lydia Sohn,
Dan Fletcher (BioE)

GigaPan: WallerLab_Berkeley
Open-source : www.laurawaller.com
Twitter: @optrickster
Github: Waller_Lab

